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# COUPLING OF METEOROLOGY AND TRACERS IN DATA ASSIMILATION SYSTEMS

Saroja Polavarapu

Climate Research Division

ECCC, Toronto, Canada

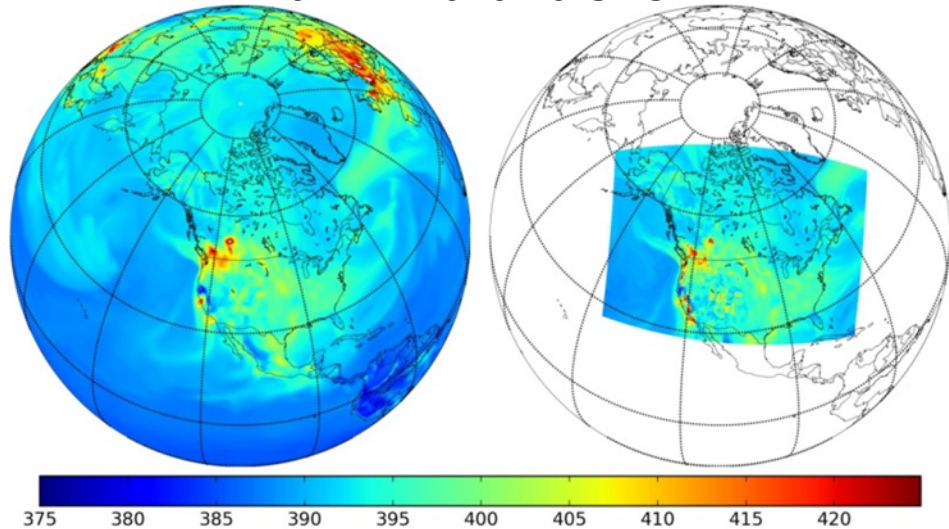
21 March 2023 BIRS Workshop



Canada 

# PERSONAL UPDATES

CO<sub>2</sub> near surface  
Jan 4. 2010 20 UTC



## Global model

- 0.9° × 0.9°
- Lid at 0.1 hPa
- CO<sub>2</sub>, CH<sub>4</sub>, CO
- 3DVar CO<sub>2</sub> DA

Model details in  
[Polavarapu et al. \(2016, ACP\)](#)

## Regional model

- 10 km grid
- Lid at 0.1 hPa
- CO<sub>2</sub>, CH<sub>4</sub>, CO

Model details in [Kim et al. \(2020, GMD\)](#),  
CO<sub>2</sub> flux inversion

[Jinwoong Kim talk](#)

- Retired from ECCO July 1, 2022
- Working a few hours per week now (institutional memory)
  - Contract renewed yearly
  - Focus on state estimation of GHG (CO<sub>2</sub>) with operational global weather forecast model. Currently: 3D-Var. Future: Add CH<sub>4</sub>, EnVar? Coupled state/flux estimation?

# OUTLINE

## Coupling of meteorology and tracers (CO<sub>2</sub>)

### 1. In the forecast model

- Conserving tracer mass
- Diagnostic: spatial scales of CO<sub>2</sub> uncertainty due to uncertain meteorology

### 2. In flux inversion

- Diagnostic: Change in CO<sub>2</sub> state due to fluxes versus uncertain meteorology

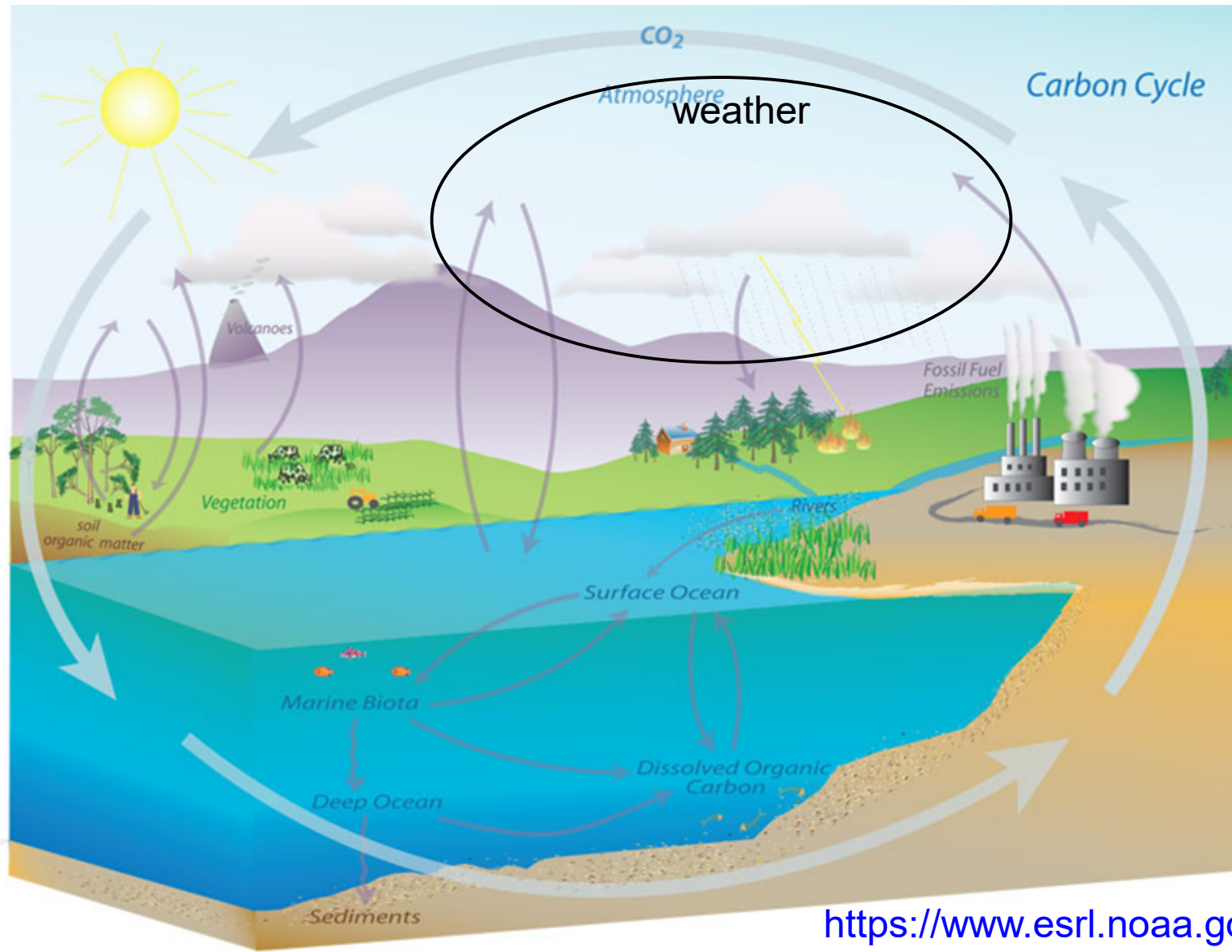
### 3. In CO<sub>2</sub> 3D-Var data assimilation

- Diagnostic: Global mass evolution?
-

# **1. THE FORECAST MODEL**

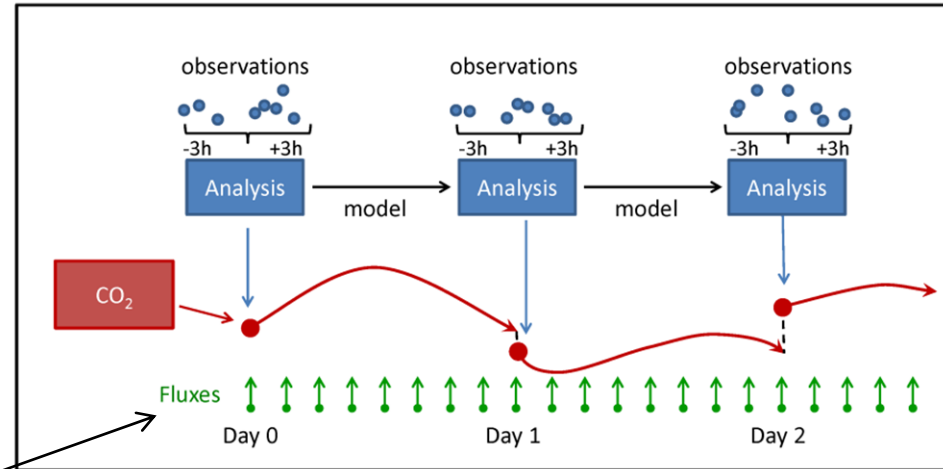
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# COUPLED LAND/OCEAN/ATMOSPHERE



# COUPLED GLOBAL WEATHER AND GREENHOUSE GAS MODELS

Initial CO<sub>2</sub> on  
1 Jan 2009 from  
CarbonTracker



Sub-daily fluxes (biospheric, ocean, anthropogenic, biomass burning)  
3-hourly fluxes from NOAA CarbonTracker (CT2013B, CT2019B)

Global coupled weather-GHG models include:

- ECMWF CAMS (Agusti-Panareda et al. 2014)
- ECCO (Polavarapu et al. 2016)
- NASA GMAO (Weir et al. 2021)
- NOAA GML (Bruhwiler, BIRS presentation 2023)

# COUPLED METEOROLOGY AND CHEMISTRY

- Meteorological model equations (momentum, thermodynamic, equation of state)
- Species continuity equation for mixing ratio:

$$c = \frac{m_c}{m_a}$$

mass  
↓  $m_c$  species  
↓  $m_a$  moist air

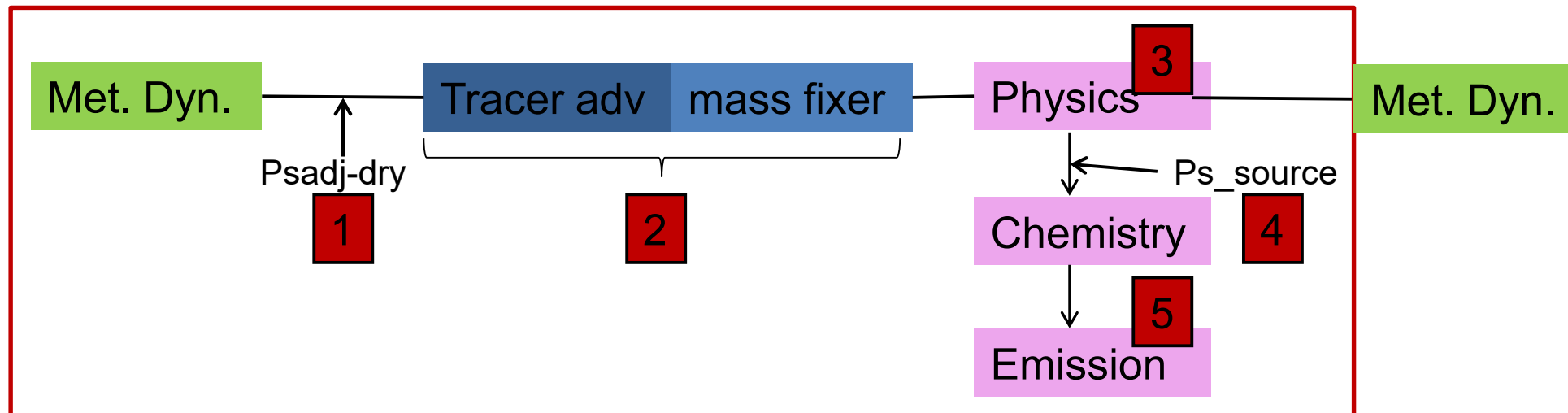
$$\frac{\partial c}{\partial t} + (\mathbf{U} \cdot \nabla)c = \frac{1}{\rho_a} \nabla \cdot (\rho_a K \nabla c) + \sum_i S_i$$

Density moist air →  $\rho_a$ 
 $\uparrow$  Diffusion coefficient
 $\left( S_i \right)$  ← emission, dry deposition, wet deposition, photochemistry, gas/particle partitioning, etc.

- For greenhouse gases: tracer mass conservation desired
- Tracer variable: dry air mixing ratio is desired

# CONSERVING TRACER MASS IN GEM

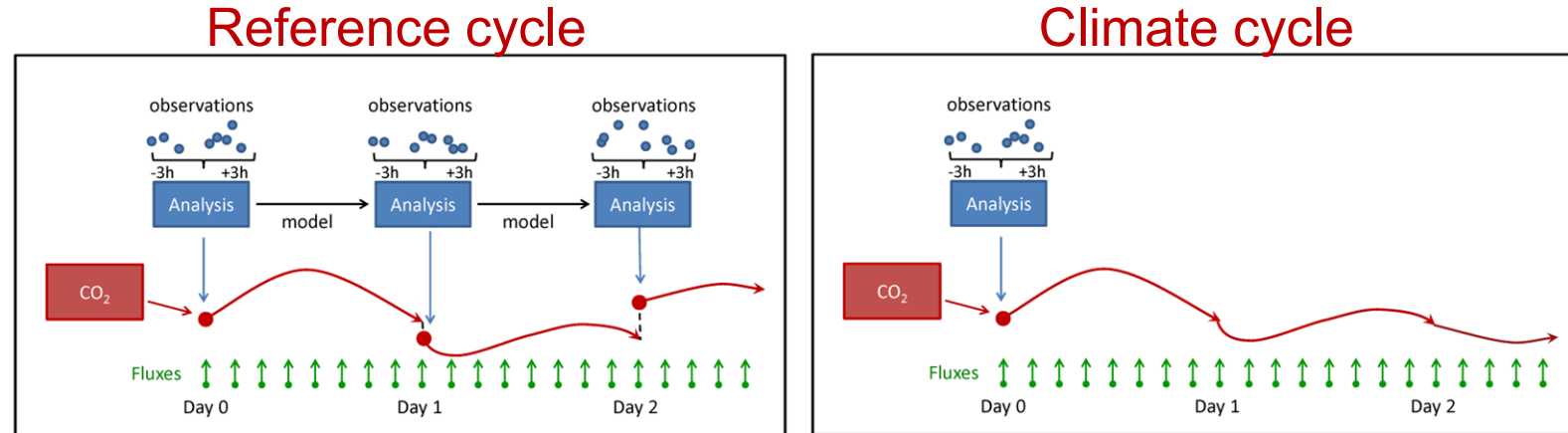
One time step



1. The model loses mass during the dynamics step, so  $ps_{adj-dry}$  adjusts the global dry air mass so it is conserved. The tracer mixing ratio is not adjusted even though the dry air mass is not locally conserved.
2. Tracer mass is changed during advection so the mass fixer is applied for global conservation. This requires knowledge of the dry air mass field ( $P_s, q$ )
3. During Physics, water vapour ( $q$ ) is changed so dry air is changed so tracer needs adjusting.
4. Mass change due to change in  $q$  from physics is added to  $P_s$ .
5. Emission is added so the tracer mass changes.  $q$  and  $P_s$  are needed.

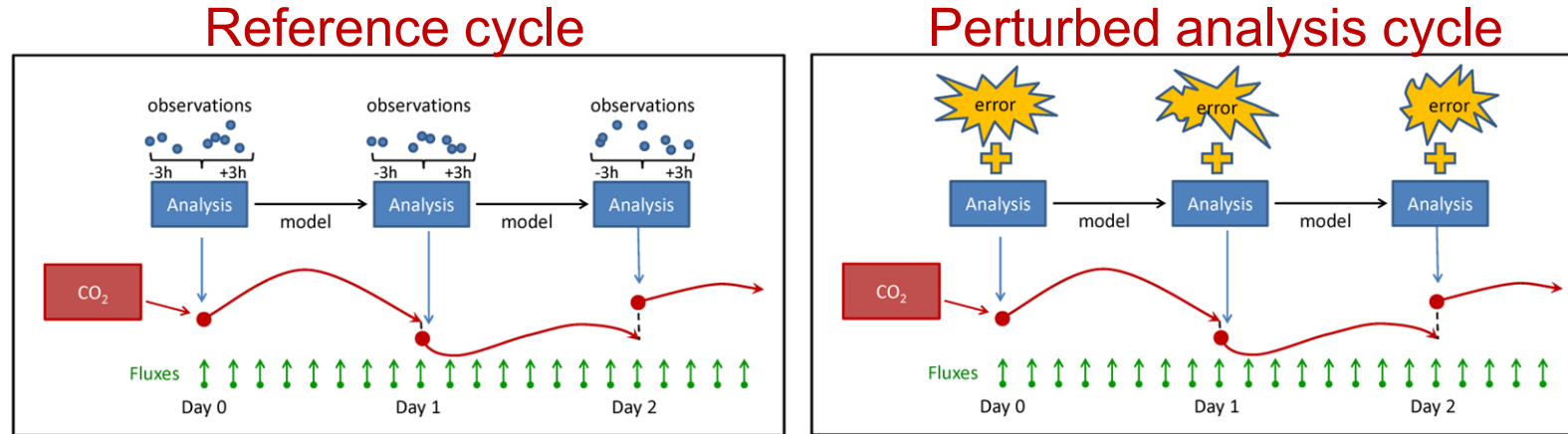


# EXPERIMENTAL DESIGN: PREDICTABILITY



- Analyses constrain CO<sub>2</sub> transport using observed meteorology even with no CO<sub>2</sub> assimilation
  - What if we don't use analyses (after the initial time) and replace them with 24h forecasts? → Climate cycle
  - Climate cycle will drift from control cycle which uses analyses
-

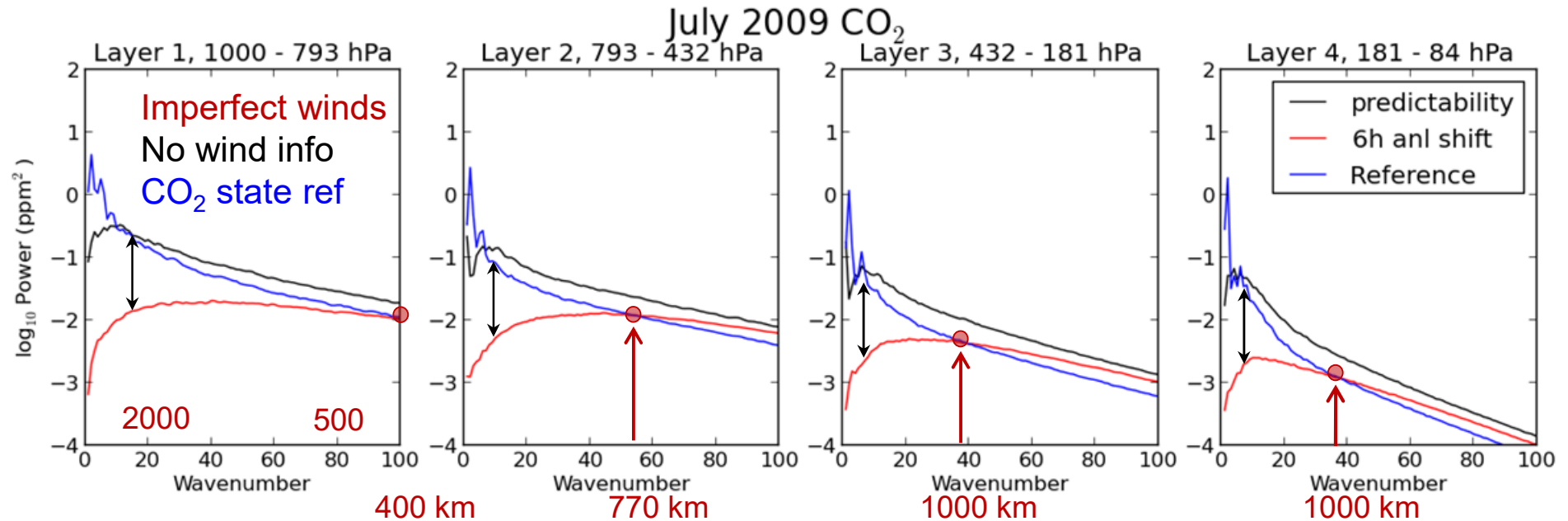
# EXPERIMENTAL DESIGN: ANALYSIS ERROR



- Climate cycle is an extreme case. In reality analyses keep our cycle close to observations. But analyses are not perfect. What is the impact of analysis error on CO<sub>2</sub> spatial scales?
  - Experiment: Perturb reference analyses by error
  - Analysis error proxy: Cycle with analysis 6h early
-

# IMPACT OF METEOROLOGICAL ANALYSIS UNCERTAINTY

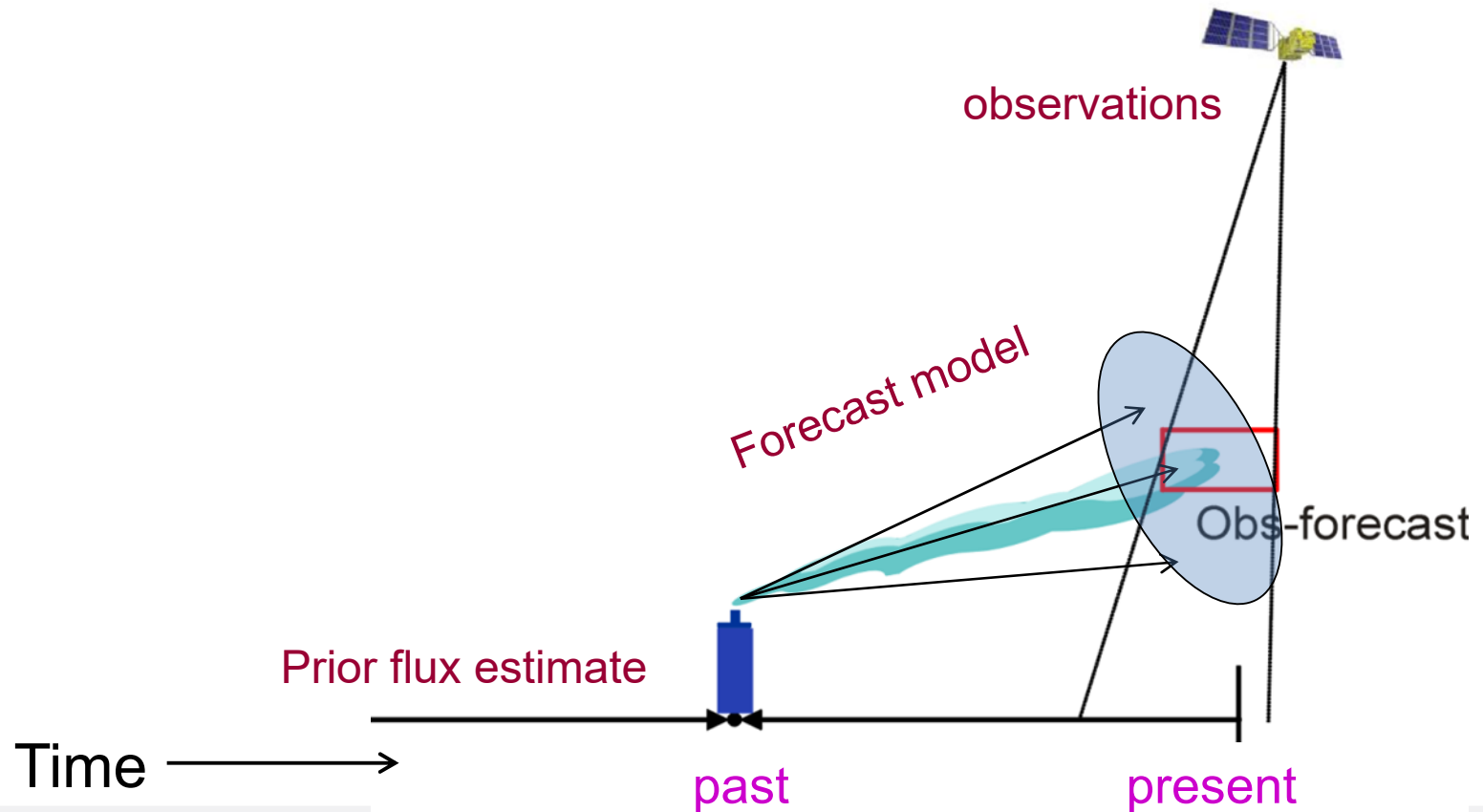
Polavarapu et al. (2016, ACP)



- Error spectra asymptote to predictability error spectra. For smaller spatial scales, we don't gain much over predictability error.
- For some wavenumber, the power in this error equals that in the state itself (red arrows). *There is a spatial scale below which CO<sub>2</sub> is not resolved due to analysis uncertainty.* This spatial scale increases with altitude.
- CO<sub>2</sub> predictability on regional scale in limited area domain (Kim et al. 2021, JGR)

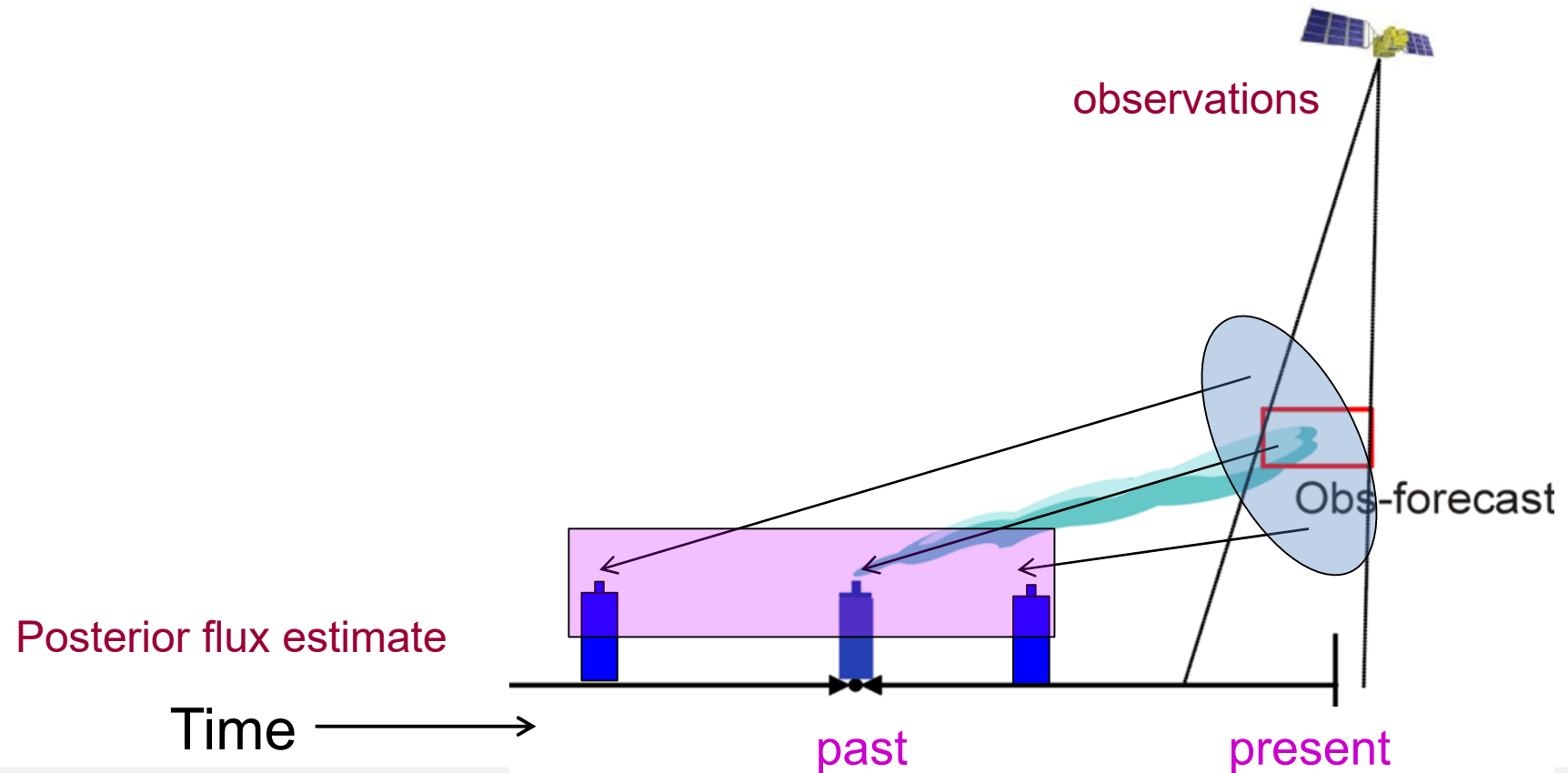
# IMPLICATIONS ON FLUX INVERSIONS

If CO<sub>2</sub> can be reliably simulated only for large spatial scales, this translates to flux uncertainties which are unaccounted for.



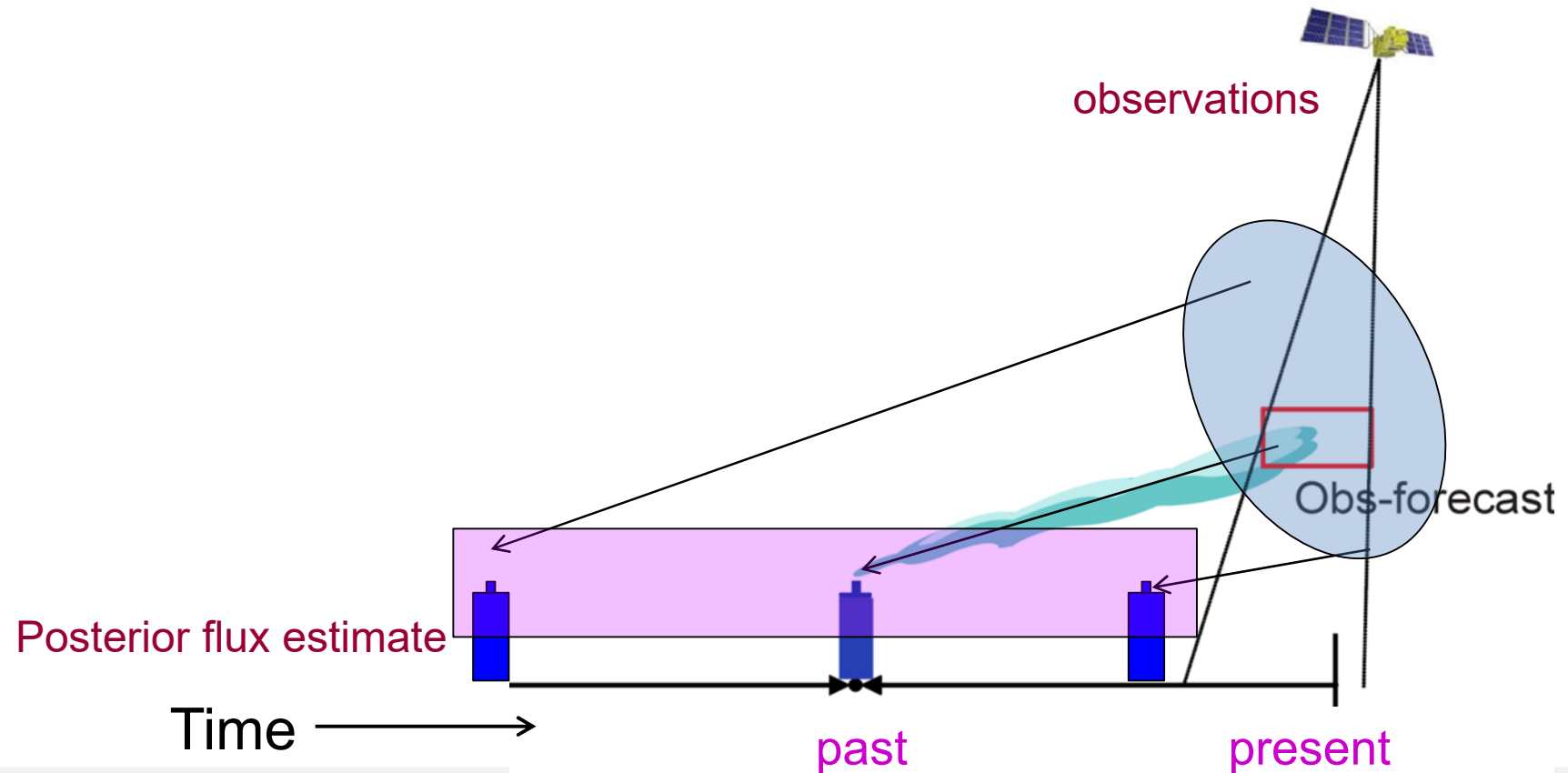
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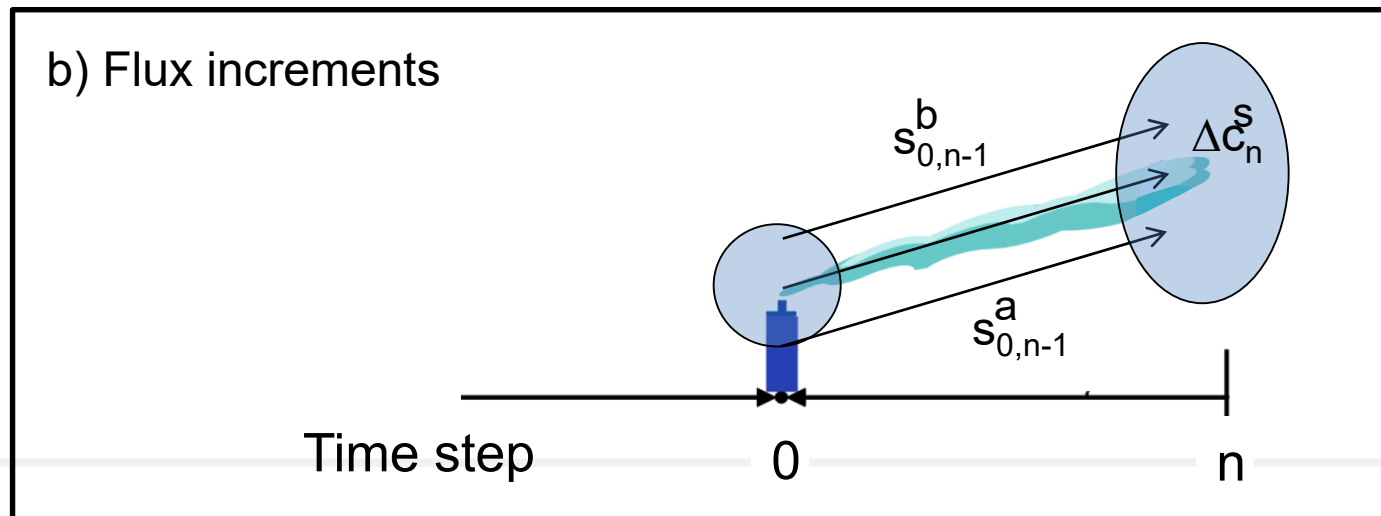
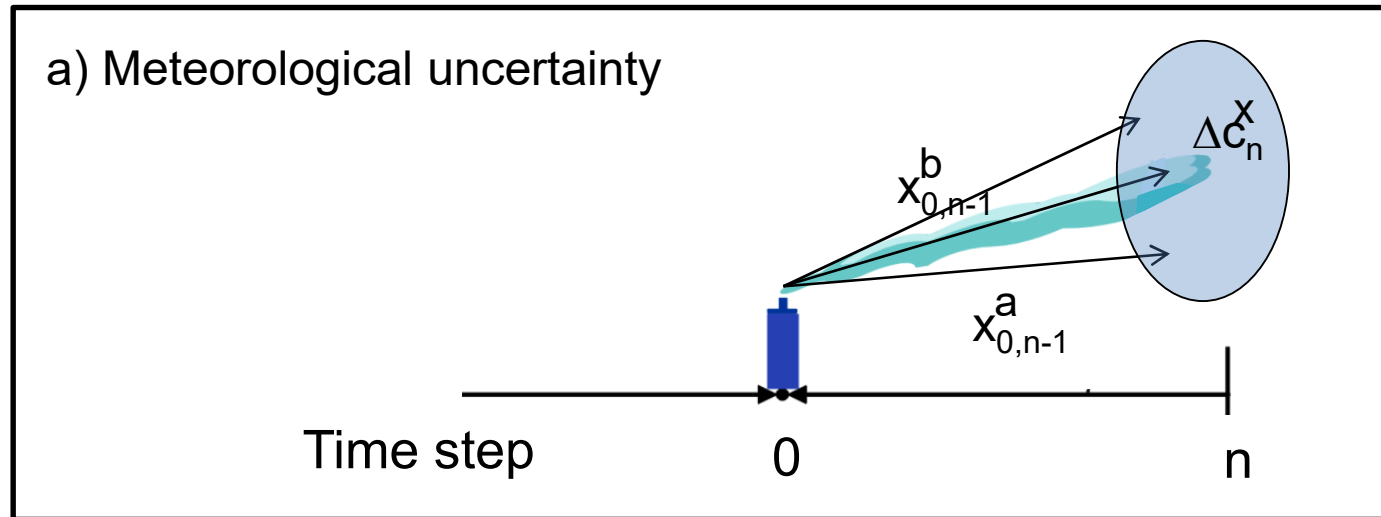
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## **2. INVERSE MODELING**

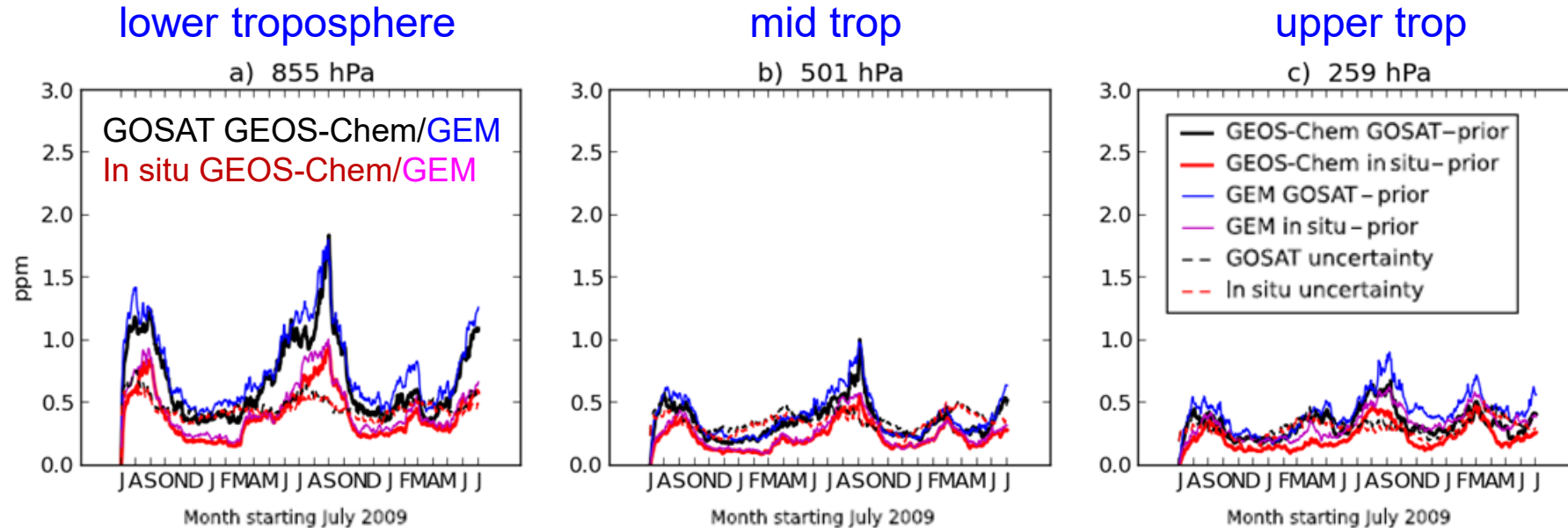
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Does the change in CO<sub>2</sub> induced by updated flux estimates exceed the uncertainty in CO<sub>2</sub> due to imperfect meteorology?





# CHANGE IN CO<sub>2</sub> DUE TO FLUX ESTIMATION



Once the flux signal has diffused to large-scale structures (~3 months in troposphere), there will be no contribution to zonal std-dev. So zonal std-dev reflects shorter time scales than zonal mean.

- CO<sub>2</sub> change due to GOSAT flux increments exceeds change in CO<sub>2</sub> due to perturbed met analyses except in boreal winter in lower trop.
- CO<sub>2</sub> change due to insitu flux increments exceeds change in CO<sub>2</sub> due to perturbed met analyses only in boreal summer in lower trop.

## **3. DATA ASSIMILATION**

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# 3D-VAR ESTIMATION OF CO<sub>2</sub> STATE

$$J_{\text{MAP}}(\mathbf{x}) = \frac{1}{2}(\mathbf{z} - \mathbf{H}\mathbf{x})^T \mathbf{R}^{-1}(\mathbf{z} - \mathbf{H}\mathbf{x}) + \frac{1}{2}(\mathbf{x} - \boldsymbol{\mu})^T \mathbf{P}^{-1}(\mathbf{x} - \boldsymbol{\mu}).$$

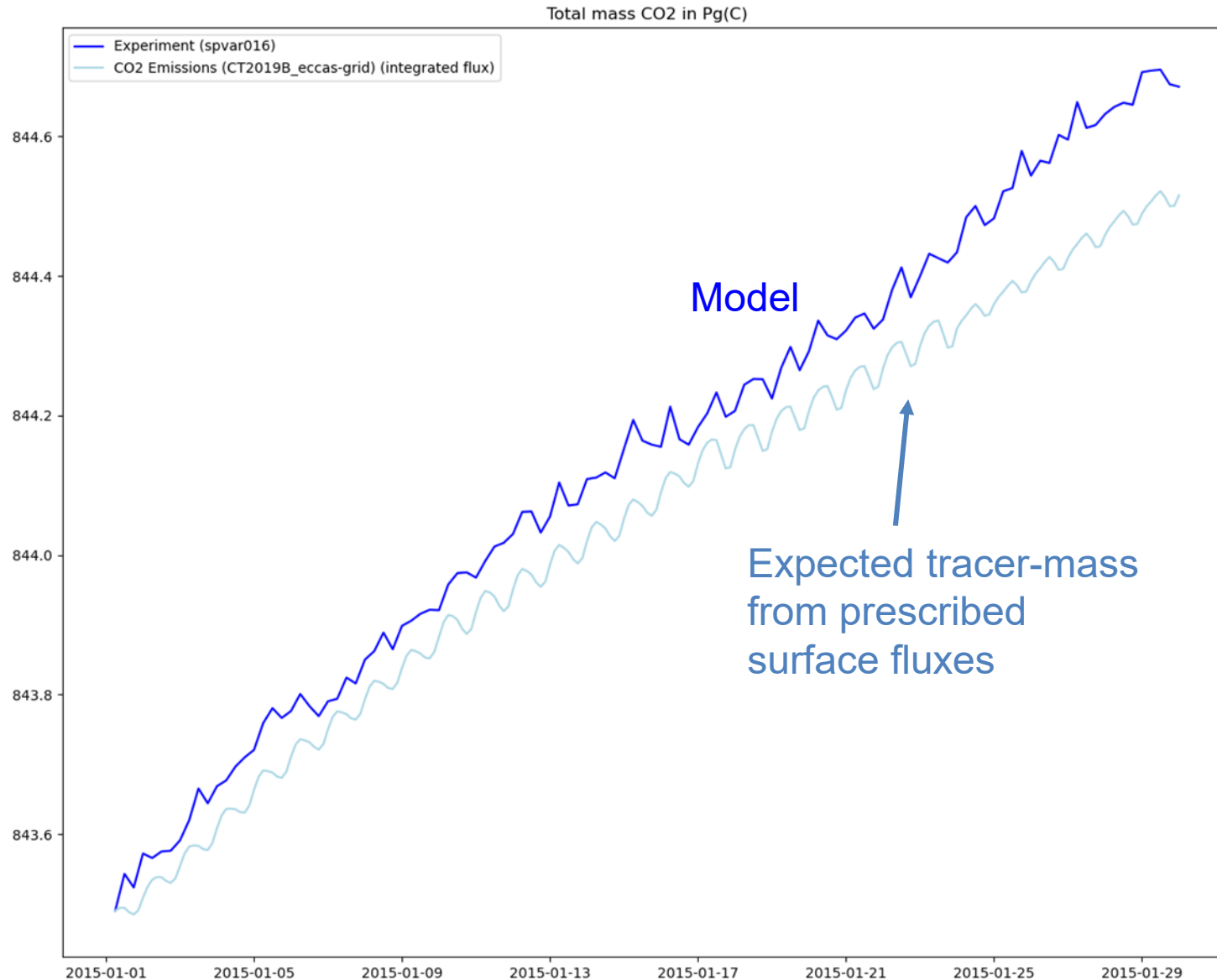
Diagram illustrating the 3D-VAR estimation of CO<sub>2</sub> state. The equation is annotated with labels:

- CO<sub>2</sub> state** (pink arrow pointing to  $\mathbf{x}$ )
- CO<sub>2</sub> obs** (pink arrow pointing to  $\mathbf{z}$ )
- Spatial interpolation** (blue arrow pointing to  $\mathbf{H}$ )
- Observation error covariance matrix** (blue arrow pointing to  $\mathbf{R}^{-1}$ )
- 6h forecast of CO<sub>2</sub>** (pink arrow pointing to  $\boldsymbol{\mu}$ )
- Forecast error covariance matrix** (blue arrow pointing to  $\mathbf{P}^{-1}$ )

- January 1-30, 2015, 6h update cycle
- **Model:** GEM-MACH-GHG 400x200 global uniform
- **CO<sub>2</sub> observations:** aircraft, surface, tower continuous obs from NOAA Obspack at all times (day and night) obspack\_co2\_1\_GLOBALVIEWplus\_v6.1\_2021-03-01
- **Obs errors:** from CT\_MDM values in ObsPack
- **Prior fluxes:** CT2019B posterior fluxes
- **Initial state:** Jan. 1, 2015 0 UTC from CT2019B molefractions
- **Background error covariance matrix:** From O<sub>3</sub> assimilation for correlations, standard deviations vary with height for 3 zonal bands: NE, TR, SE.

Previous work was with EnKF for simulated CO observations ([Khade et al. 2021](#), [GMD](#))

# Global CO<sub>2</sub> mass evolution in Jan 2015



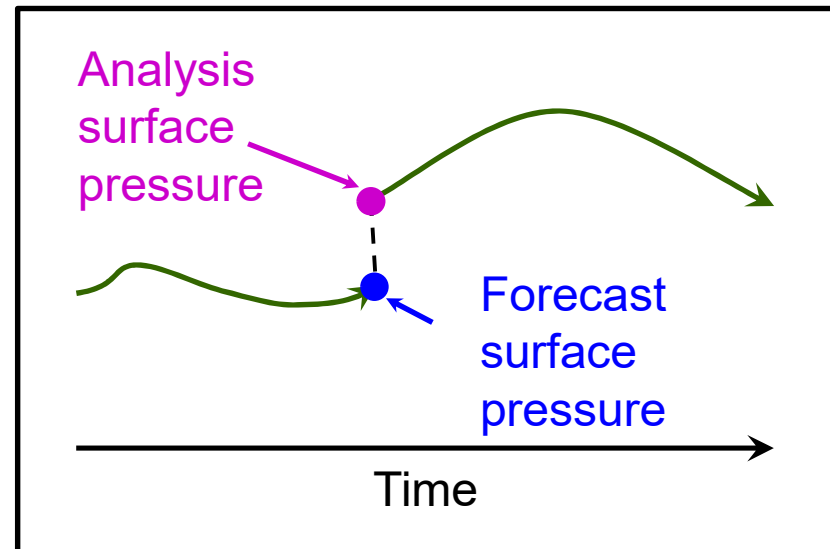
Time series of CO<sub>2</sub> global mass show departures from the mass expected from prescribed CO<sub>2</sub> surface fluxes.

This is because:

- 1) The global dry-air mass changes in the model when a new meteorological analysis is inserted every 6 h
- 2) Assimilating CO<sub>2</sub> observations will create adjustments to the CO<sub>2</sub> state and hence the global CO<sub>2</sub> mass

# DEALING WITH DRY AIR MASS CHANGES AT ASSIMILATION WINDOW INTERFACES

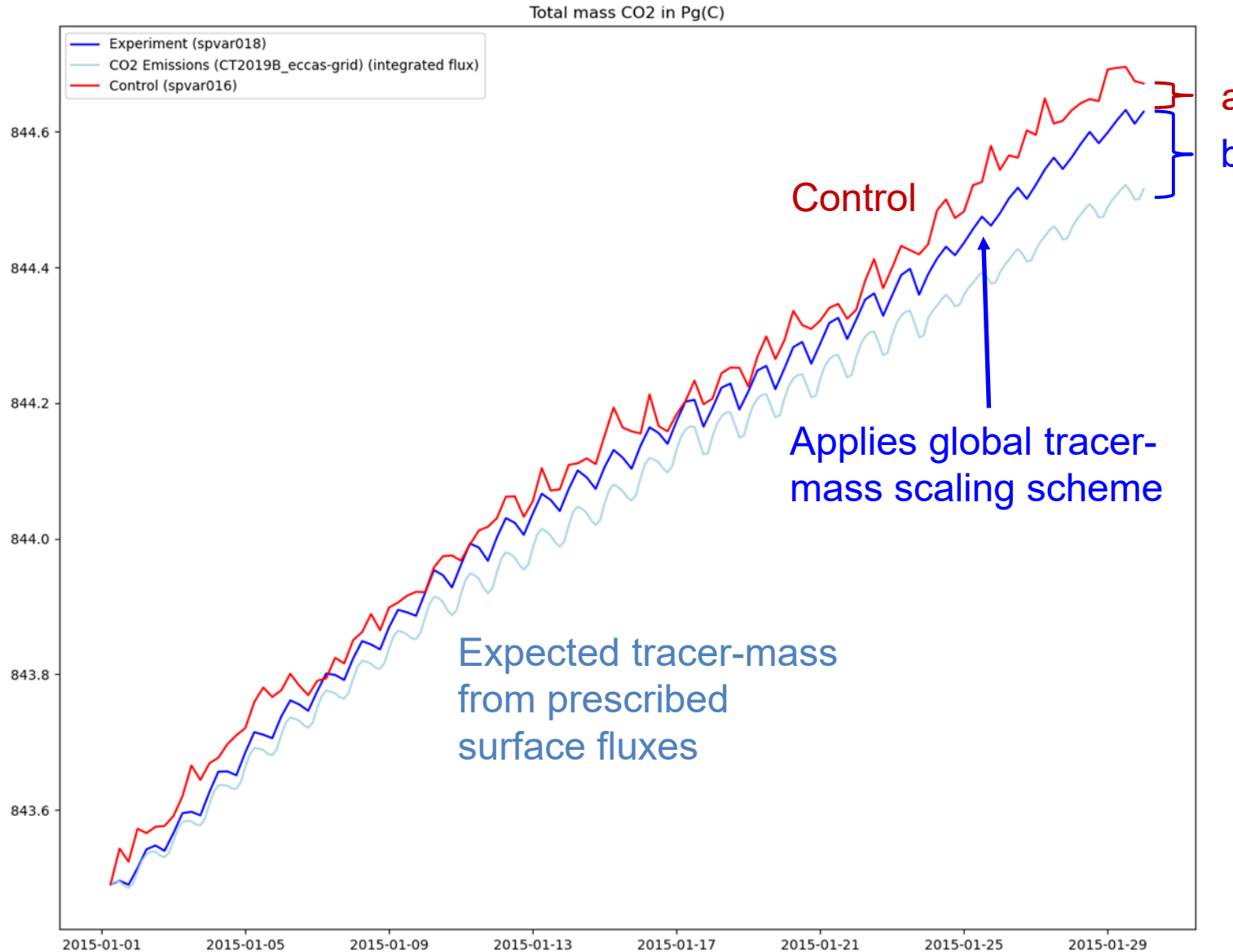
If we can account for the change in dry-air mass across the temporal boundary between analysis cycles, then we can compare the magnitude of global mass change in CO<sub>2</sub> due to dry-air mass changes in the model to the change due to assimilating CO<sub>2</sub> observations.



We want to adjust the analysis mixing ratio field by a global constant,  $\epsilon$ :

$$\tilde{c}_{i,k}^{dry,a} = c_{i,k}^{dry,a} + \epsilon = c_{i,k}^{dry,f} + \Delta c_{i,k}^{dry,a} + \epsilon$$

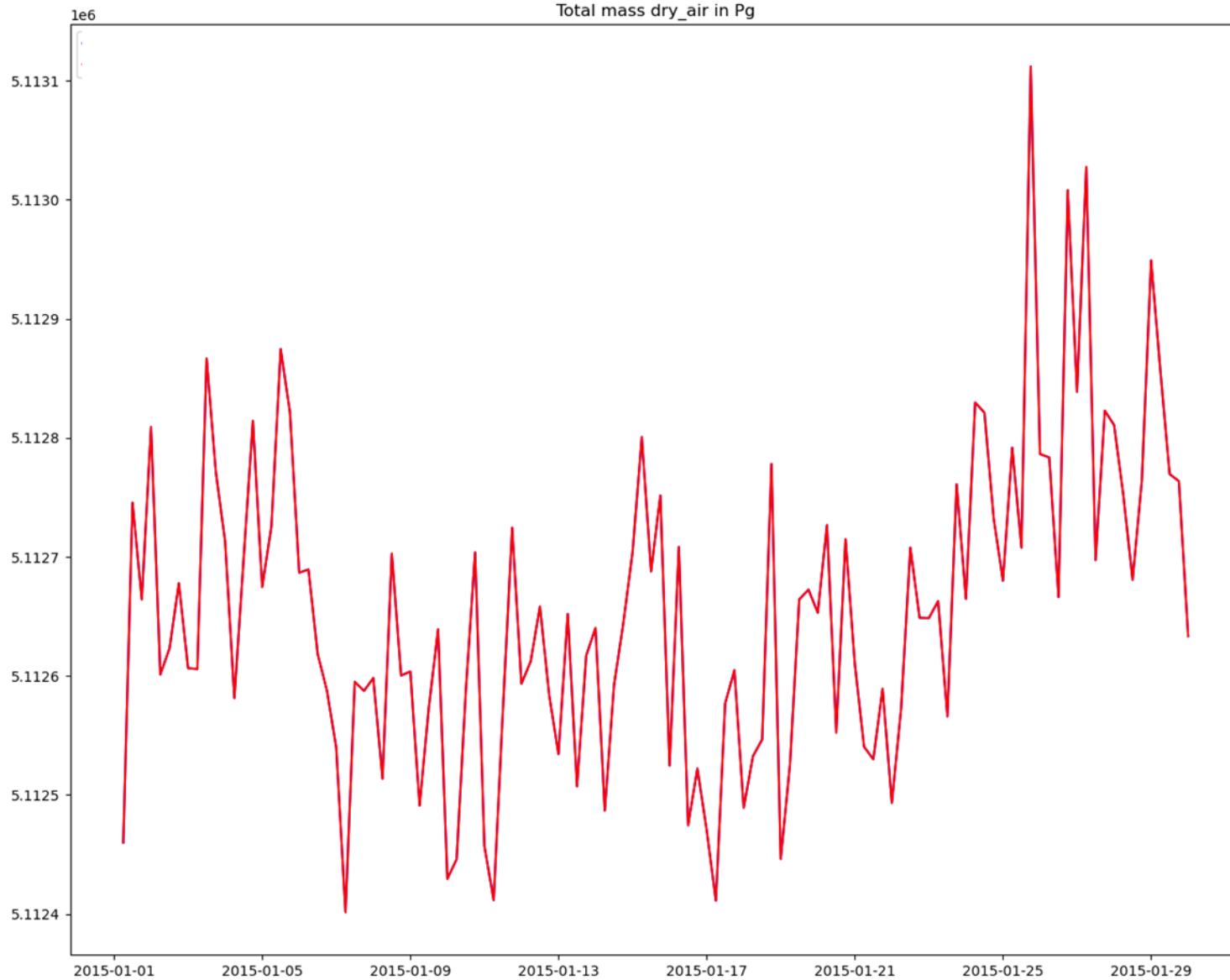
# Global CO<sub>2</sub> mass due to analysis increments



- a) Mass change due to dry-air mass adjustments
- b) Mass added through CO<sub>2</sub> data assimilation

The change in mass due to global dry-air mass adjustments (a) can exceed that due to assimilation of CO<sub>2</sub> data (b)

# Global dry air mass in GEM



Jan 1

Jan 29

Trenberth and Smith (2005, J.Clim):

**Global dry air mass**

$(5.132 \pm 0.005) \times 10^{18}$  kg

**Global water vapor:**

$(1.25 \pm 0.1) \times 10^{16}$  kg

Y-axis range is  $0.0007 \times 10^{18}$  kg

Ticks are  $0.0001 \times 10^{18}$  kg

# SUMMARY

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### 1. In the forecast model

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### 2. In flux inversion

- Diagnostic: Change in CO<sub>2</sub> state due to fluxes versus uncertain meteorology

### 3. In CO<sub>2</sub> 3D-Var data assimilation

- Diagnostic: Global mass evolution

## Feedback?

Contact: [saroja.polavarapu@ec.gc.ca](mailto:saroja.polavarapu@ec.gc.ca), Teams, Zoom, etc.

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# REFERENCES

- Polavarapu, S.**, M. Neish, M. Tanguay, C. Girard, J. de Grandpre, K. Semeniuk, S. Gravel, S. Ren, S. Roche, D. Chan, K. Strong: *The impact of meteorological analysis uncertainties on the spatial scales resolvable in CO2 model simulations.* *Atmos. Chem. Phys.* **16**, 12005-12038, <https://doi.org/10.5194/acp-16-12005-2016> , 2016.
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