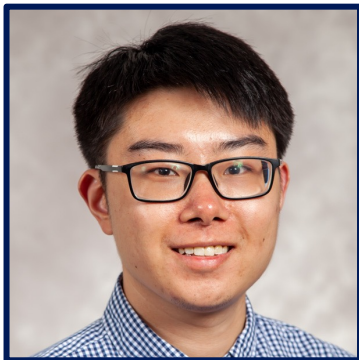


Concept Whitening for Interpretable Image Recognition

Interpretable ML Lab, Duke University



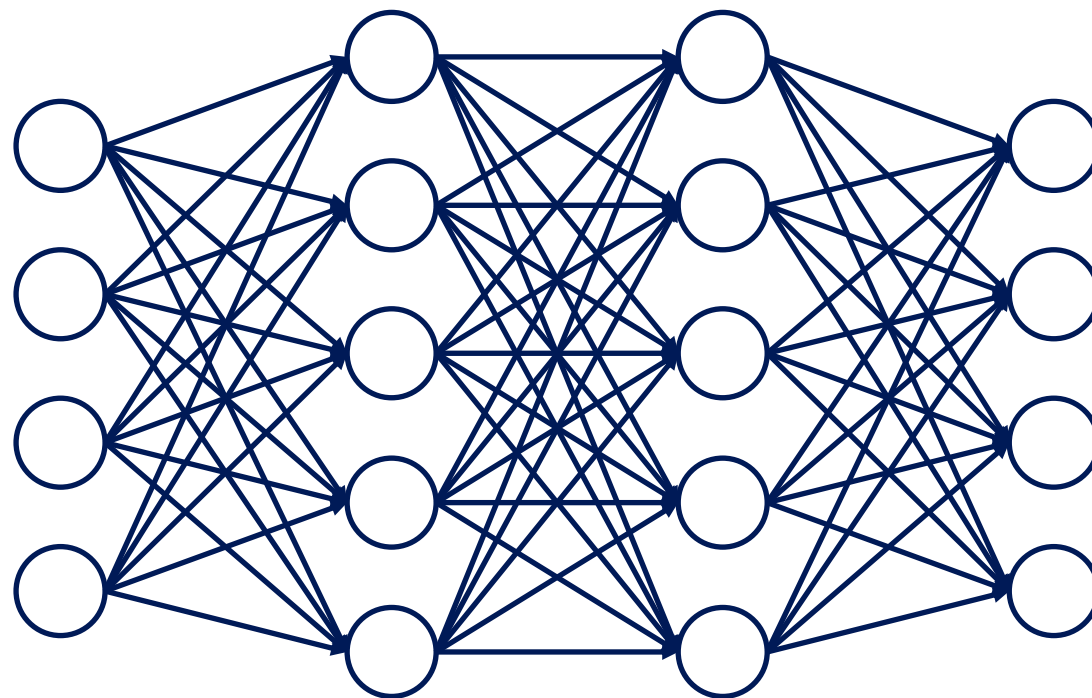
Zhi Chen



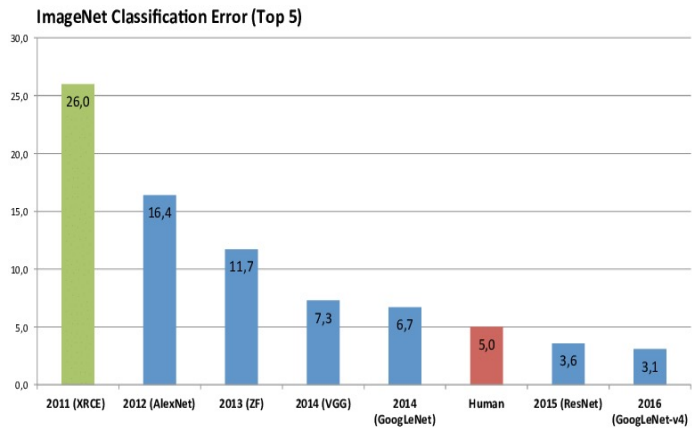
Yijie Bei



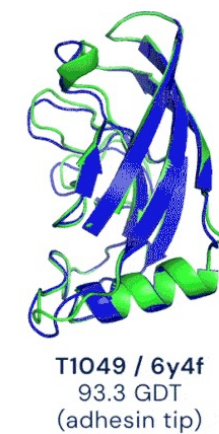
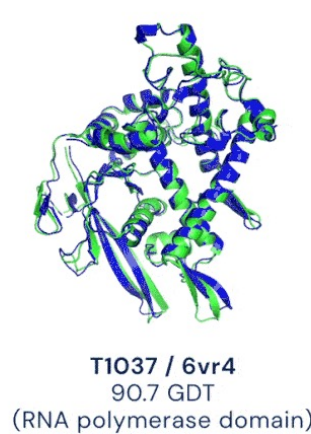
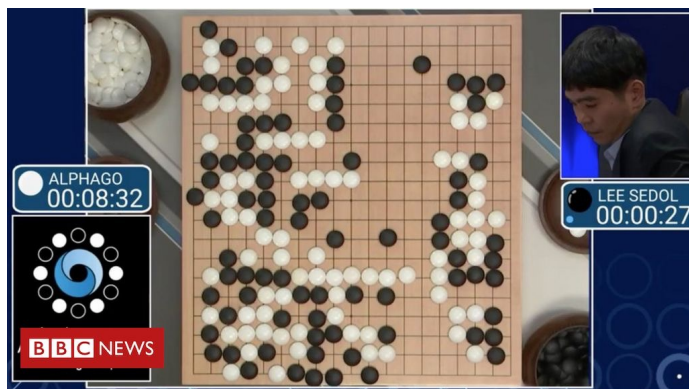
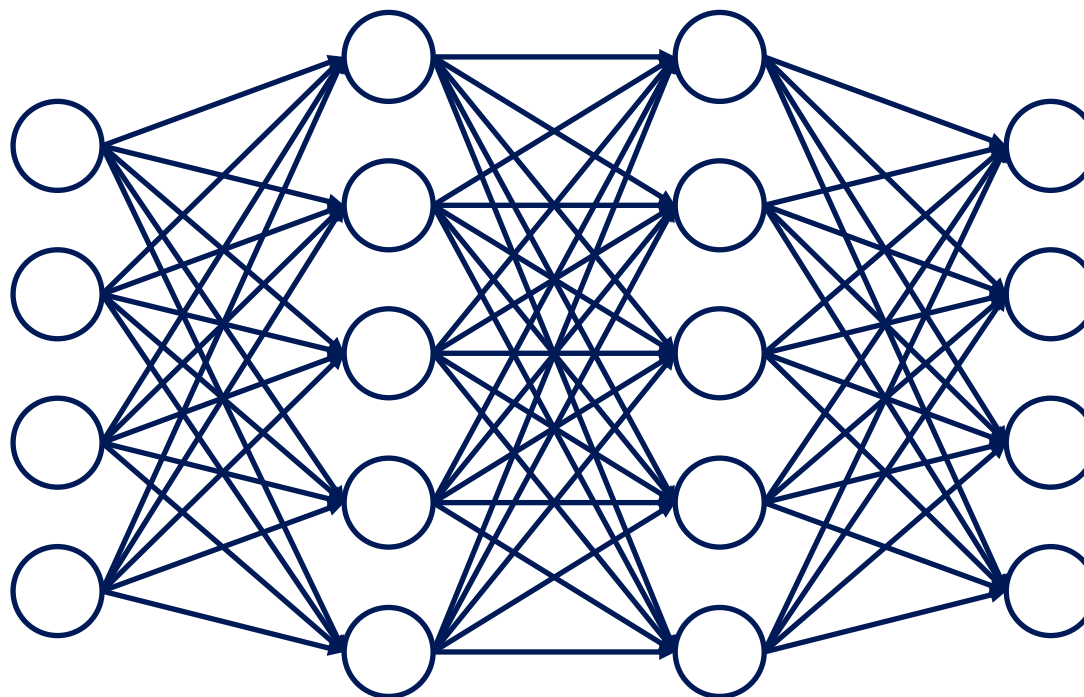
Cynthia Rudin

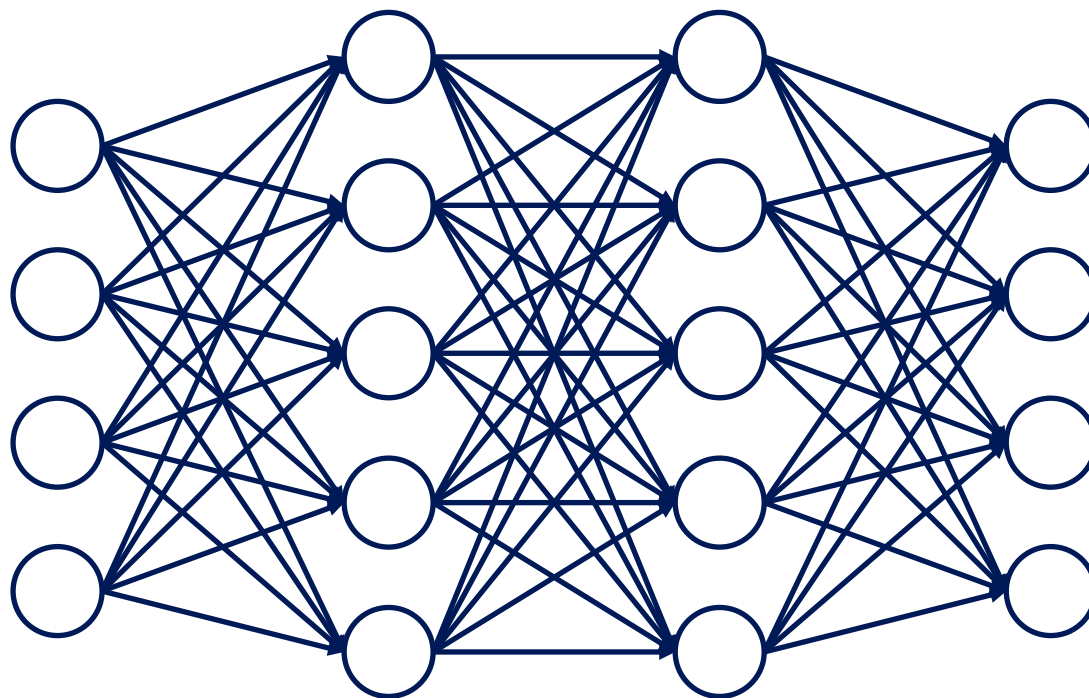


Duke



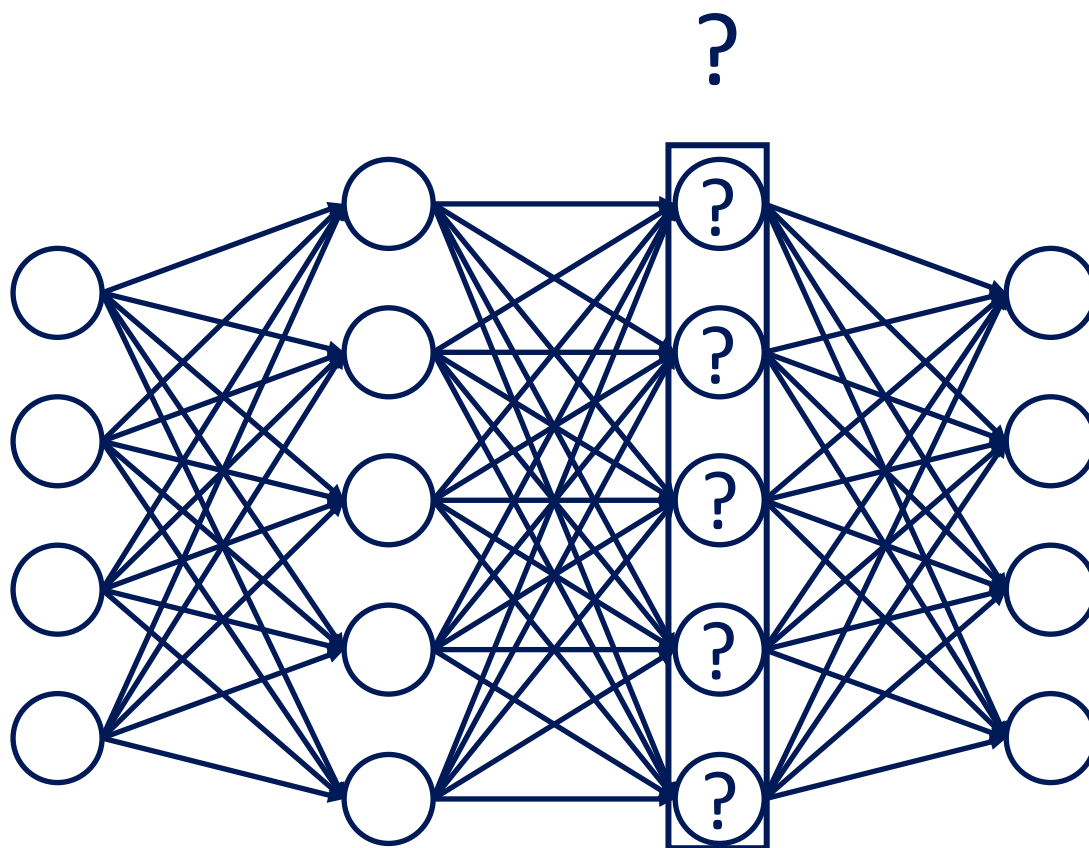
Great success !!!





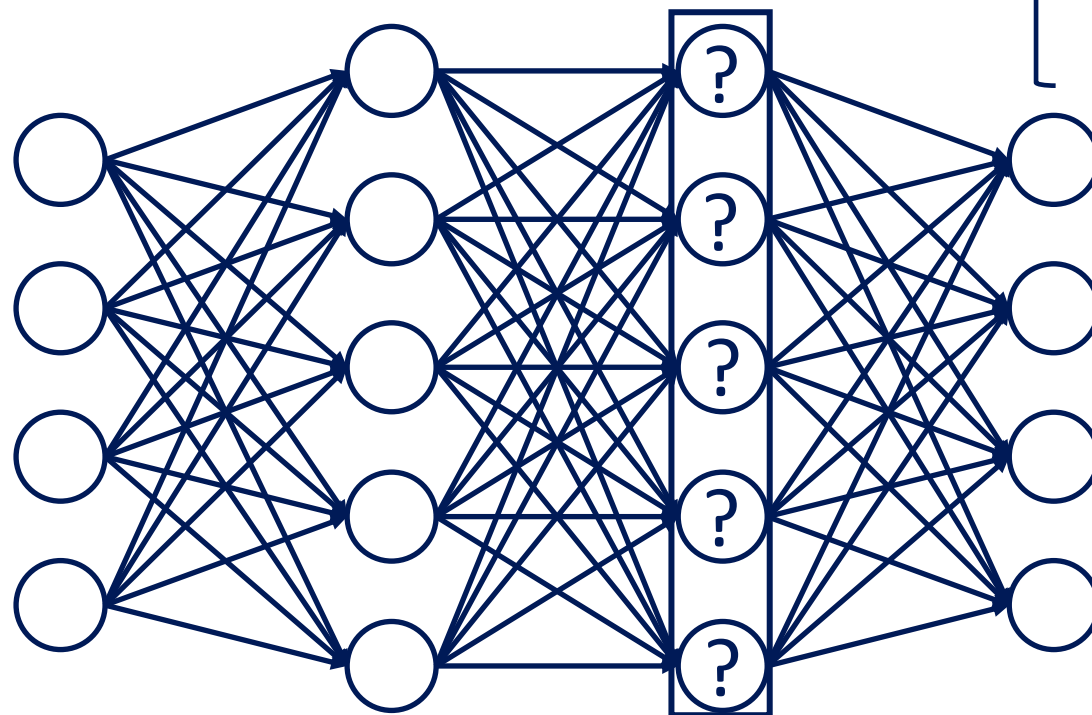
sunset

Duke



sunset

Duke

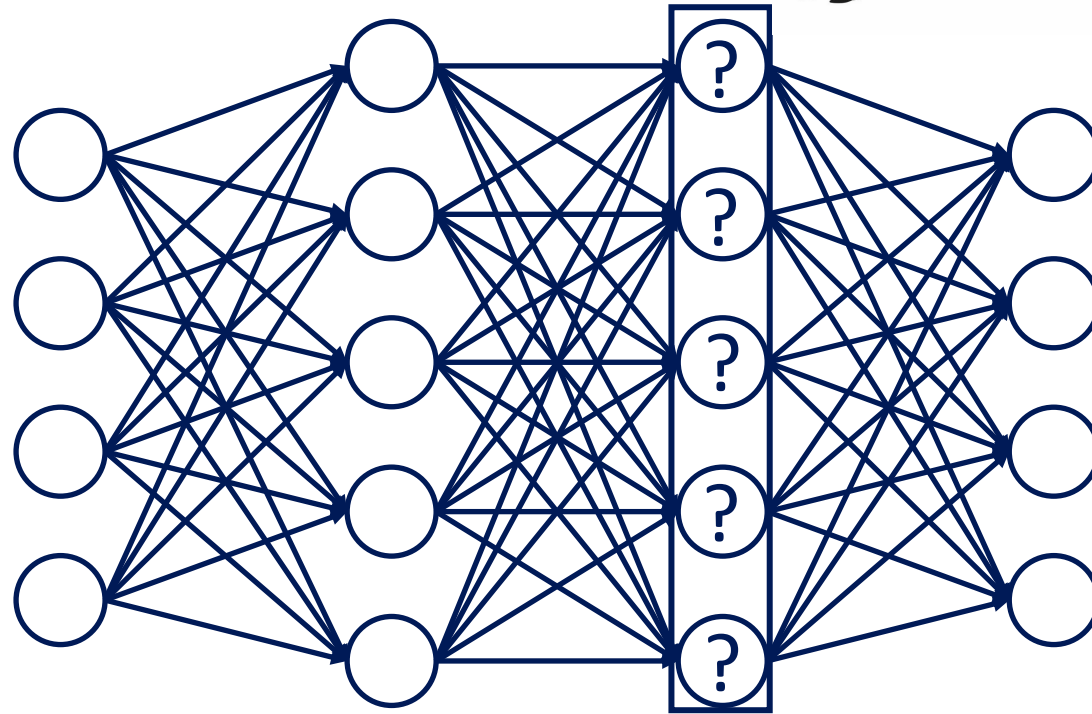


interpretability

- 1. build trust
- 2. debug models
- 3. gain knowledge
- ...



sunset



post hoc analysis

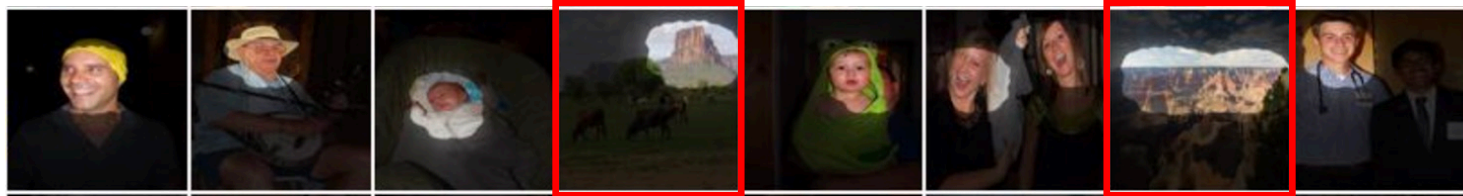


sunset

concept based - human reason in concepts

Post hoc analysis – concept based

- Single neuron (Zhou et al, 2014; 2018)

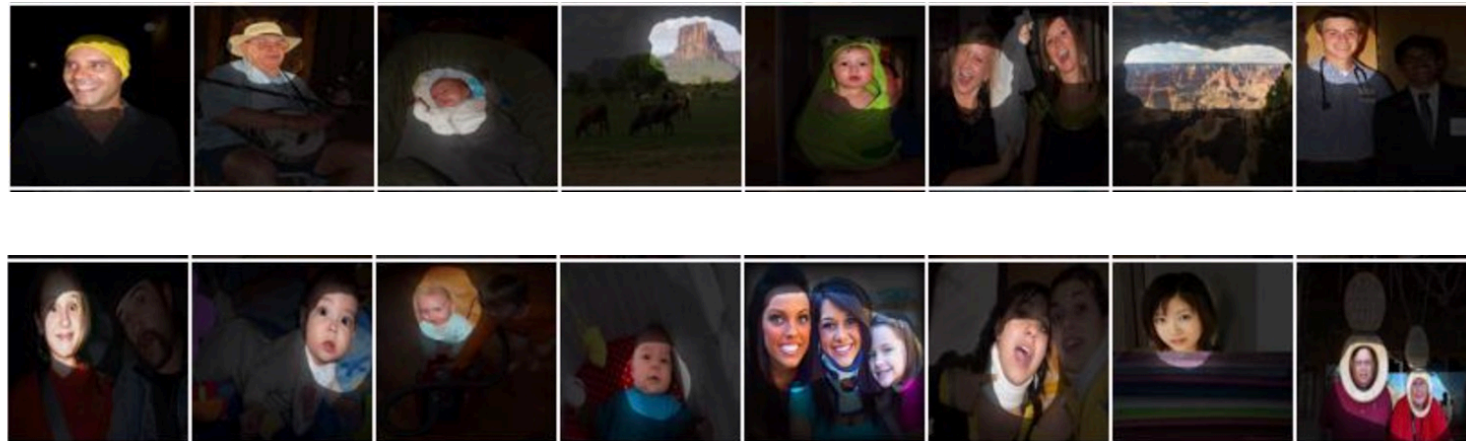


neuron 1

impure!

Post hoc analysis – concept based

- Single neuron (Zhou et al, 2014; 2018)



neuron 1

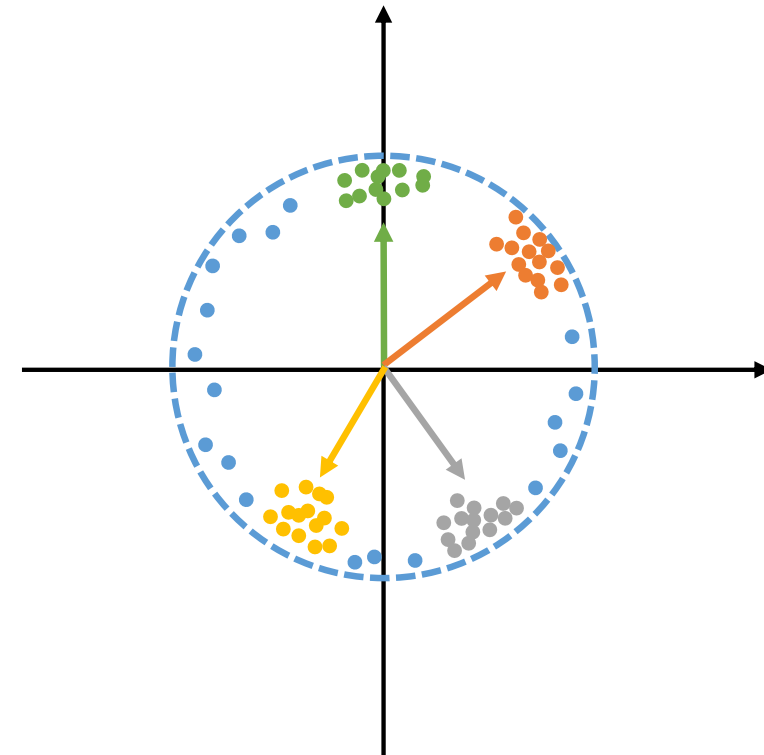
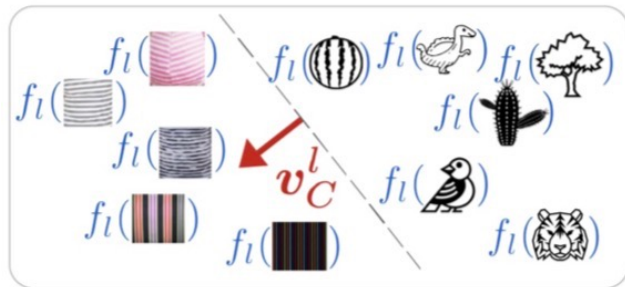
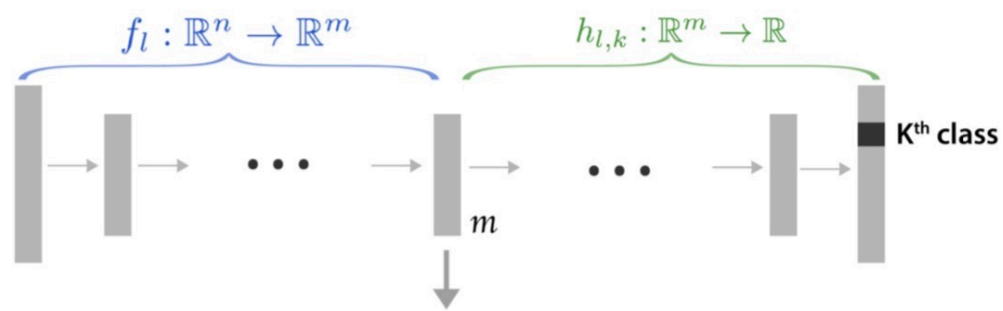
neuron 2

distributed!

single neuron of standard NN ~~→~~ single concept

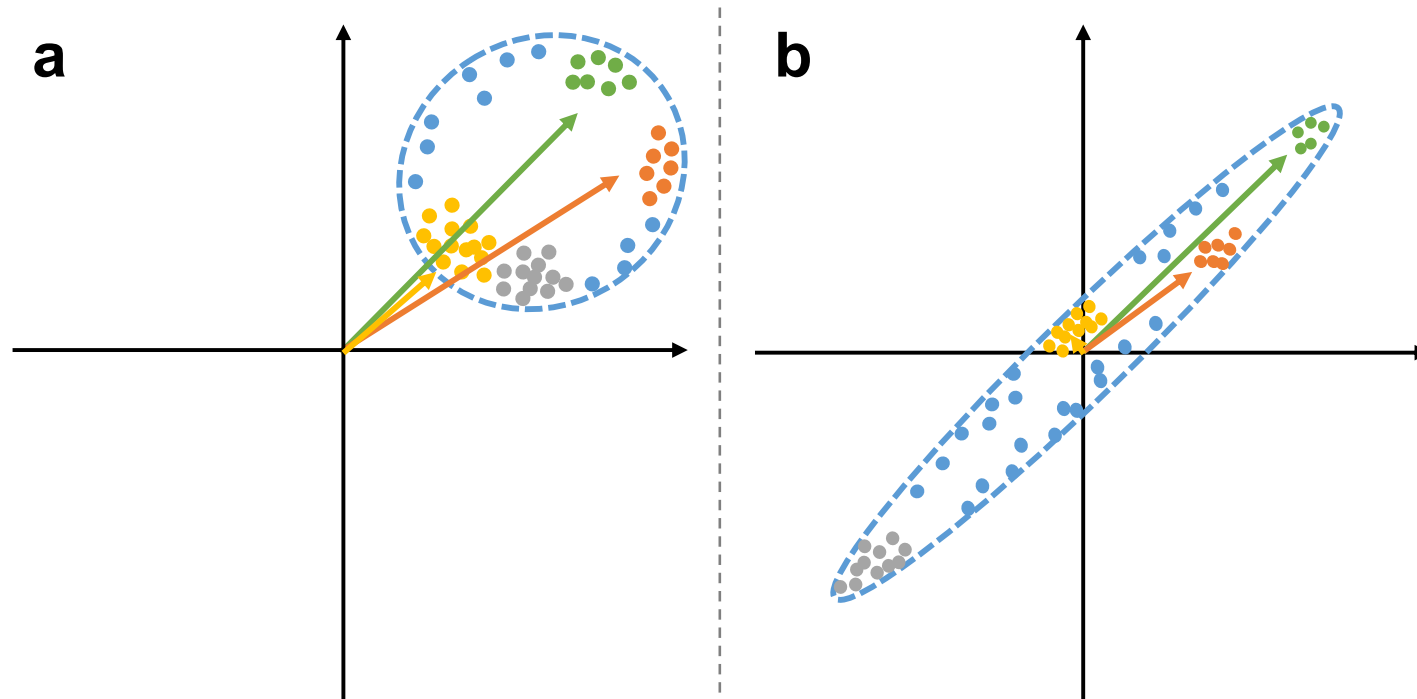
Post hoc analysis – concept based

- Linear combination of neurons (Kim et al, 2017; Zhou et al, 2018)
 - better than single neuron
 - assume all concepts are separated



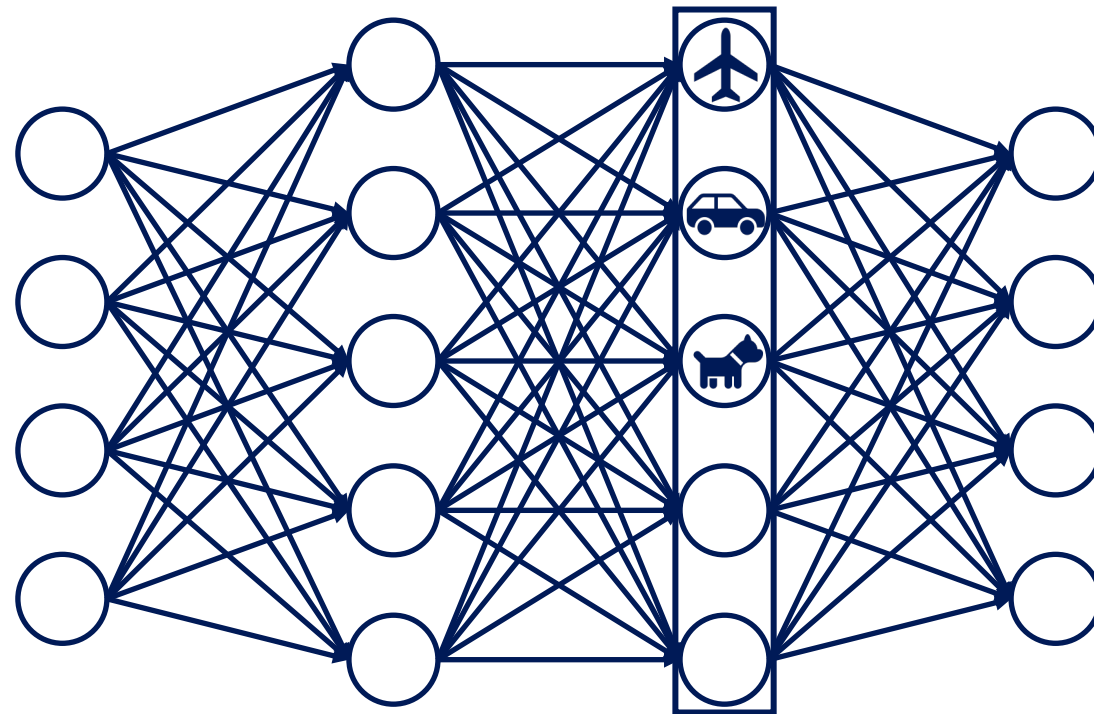
Post hoc analysis – concept based

- Linear combination of neurons (Kim et al, 2017; Zhou et al, 2018)
 - reality: concept vectors may point to the same direction



The idea

- Why not do it by ourselves?
- Create a disentangled latent space that its axes represent known concepts

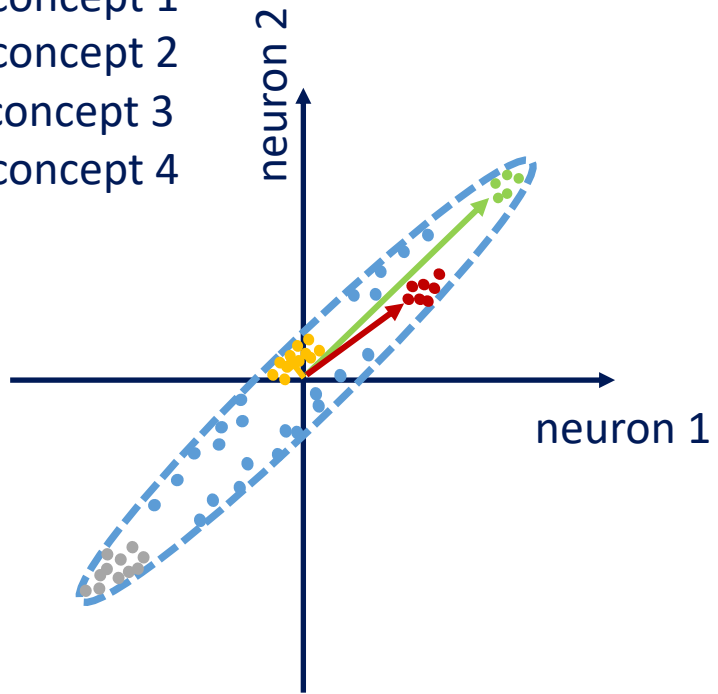


Concept Whitening

- Step 1: Whitening transformation
 - Decorrelate the latent space
 - Separate the concepts
- Step 2: Rotation transformation
 - Align the concepts to corresponding axes
 - Maintain the decorrelation property

Concept Whitenening

- concept 1
- concept 2
- concept 3
- concept 4

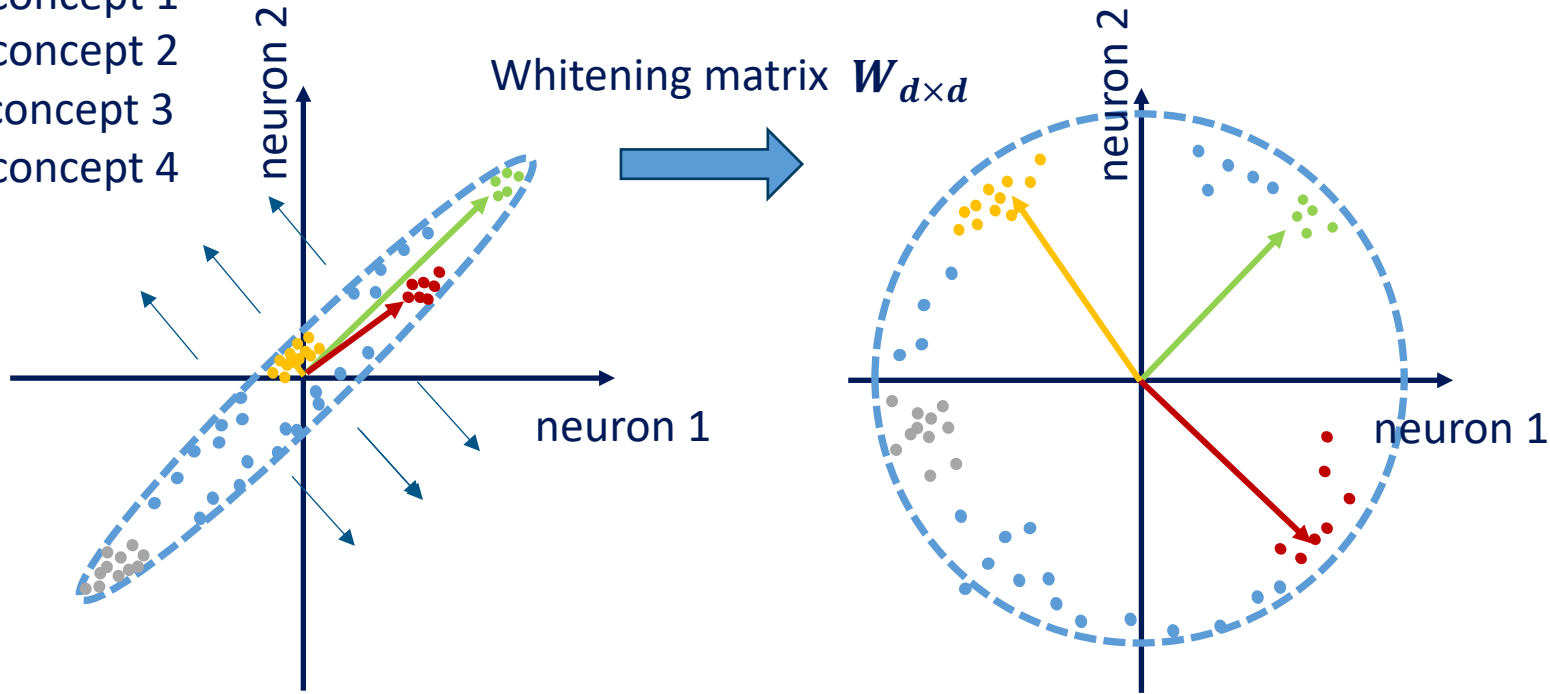


Mean-centered latent features

$$\tilde{\mathbf{Z}}_{d \times n} = \mathbf{Z}_{d \times n} - \boldsymbol{\mu} \mathbf{1}_{n \times 1}^T$$

Concept Whitenening

- concept 1
- concept 2
- concept 3
- concept 4



Mean-centered latent features

$$\tilde{\mathbf{Z}}_{d \times n} = \mathbf{Z}_{d \times n} - \boldsymbol{\mu} \mathbf{1}_{n \times 1}^T$$

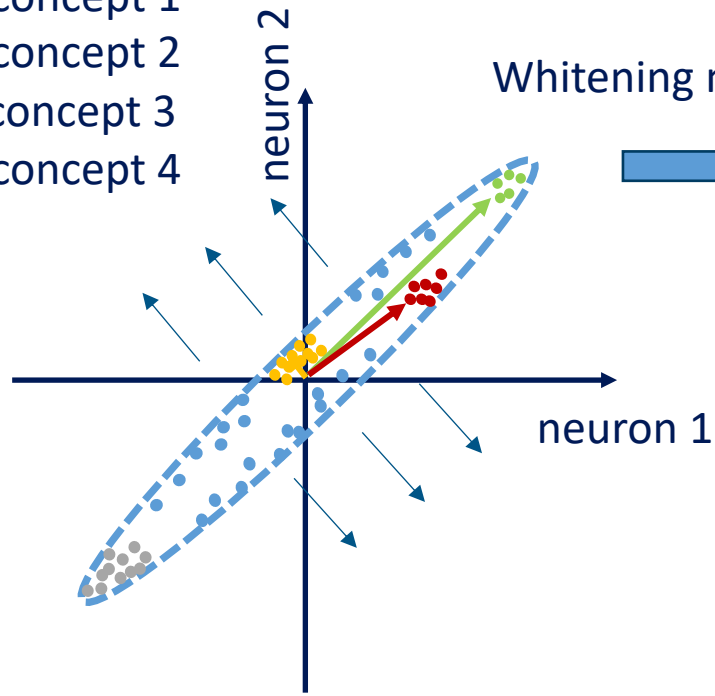
After whitening transformation

$$\mathbf{W} \tilde{\mathbf{Z}}$$

$$\mathbf{W} \text{ should obey } \mathbf{W}^T \mathbf{W} = \left(\frac{\tilde{\mathbf{Z}} \tilde{\mathbf{Z}}^T}{n} \right)^{-1}$$

Concept Whitenening

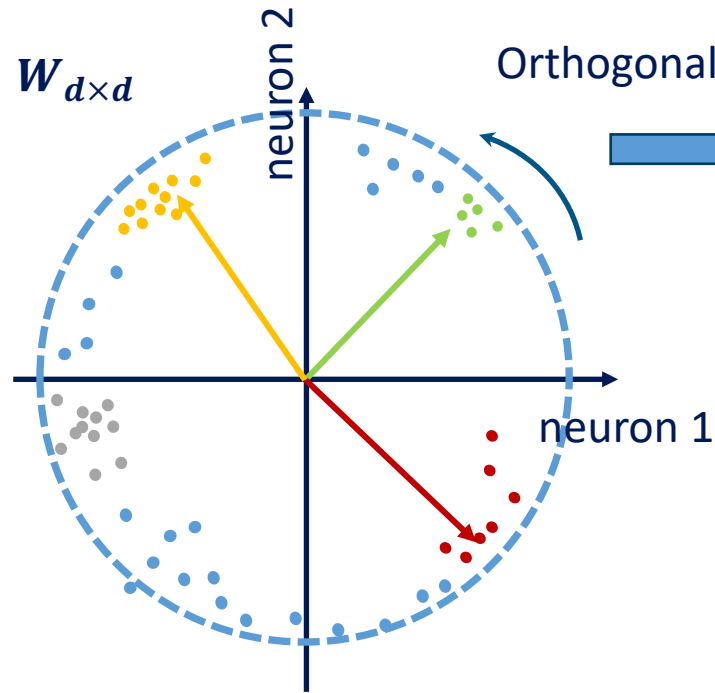
- concept 1
- concept 2
- concept 3
- concept 4



Mean-centered latent features

$$\tilde{\mathbf{Z}}_{d \times n} = \mathbf{Z}_{d \times n} - \boldsymbol{\mu} \mathbf{1}_{n \times 1}^T$$

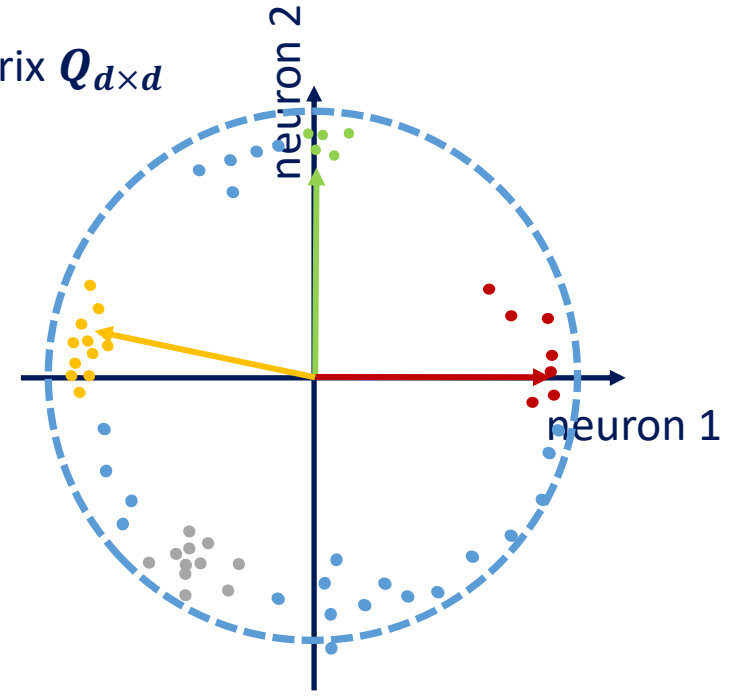
Whitening matrix $\mathbf{W}_{d \times d}$



After whitening transformation

$$\mathbf{W} \tilde{\mathbf{Z}}$$

Orthogonal matrix $\mathbf{Q}_{d \times d}$



After rotation transformation

$$\mathbf{Q}^T \mathbf{W} \tilde{\mathbf{Z}}$$

Duke

\mathbf{W} should obey $\mathbf{W}^T \mathbf{W} = \left(\frac{\tilde{\mathbf{Z}} \tilde{\mathbf{Z}}^T}{n} \right)^{-1}$

$\mathbf{W}' = \mathbf{Q}^T \mathbf{W}$ is also a whitening matrix

Learning the parameters

- Sample mean $\boldsymbol{\mu}$ and whitening matrix \mathbf{W}
 - Training phase: compute on the fly, support back-propagation (Huang et al)
 - Testing phase: exponential moving average of mini-batches (Ioffe & Szegedy)
- Orthogonal matrix \mathbf{Q}
 - maximizing concept activation under orthogonality constraint

$$\max_{\mathbf{q}_1, \mathbf{q}_2, \dots, \mathbf{q}_k} \sum_{j=1}^k \frac{1}{n_j} \mathbf{q}_j^T \mathbf{W} \mathbf{Z}_{c_j} \mathbf{1}_{n_j \times 1}$$
$$s. t. \mathbf{Q}^T \mathbf{Q} = \mathbf{I}_d$$

\mathbf{Z}_{c_j} : samples of concept j

$\mathbf{W} \mathbf{Z}_{c_j}$: after whitening

$\mathbf{q}_j^T \mathbf{W} \mathbf{Z}_{c_j}$: projection on axis j

$\frac{1}{n_j} \mathbf{q}_j^T \mathbf{W} \mathbf{Z}_{c_j} \mathbf{1}_{n_j \times 1}$: average activation

\mathbf{Q} can be trained by gradient descent on Stiefel manifold (Wen & Yin, 2013)

What's the cost of interpretability?

Main task performance

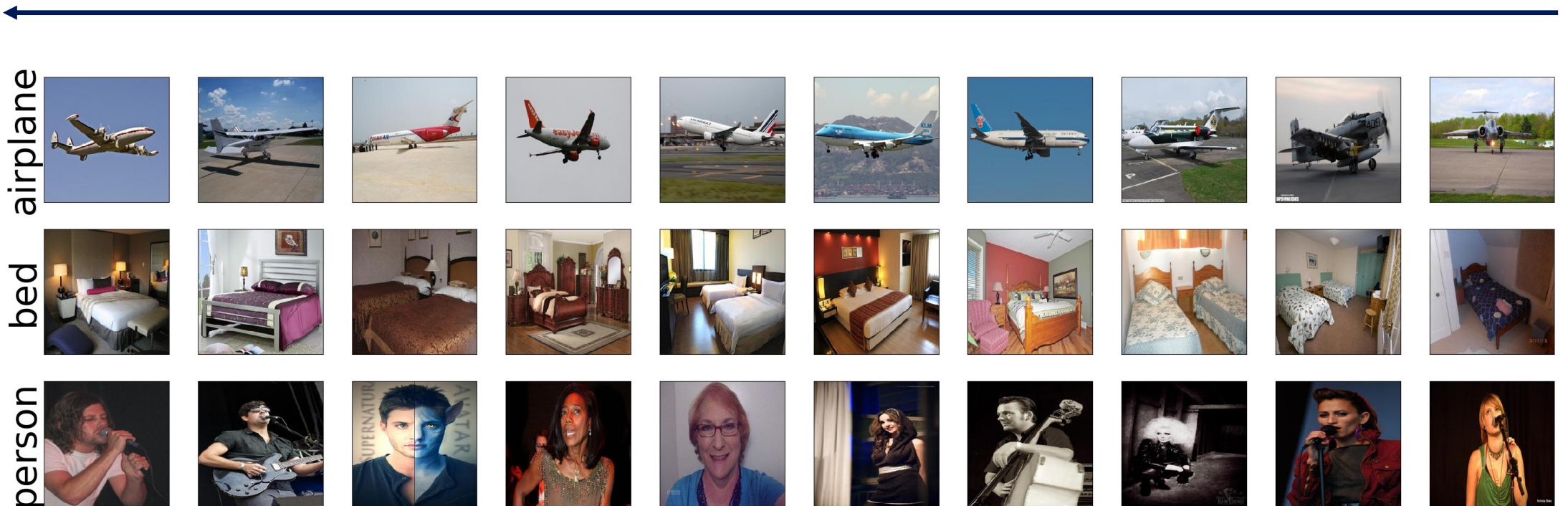
- accuracy is on par with standard CNNs
 - different datasets, backbone architectures, layers, #concepts
- warm-start from pretrained model
 - replace BN with CW
 - *only one* additional epoch of further training

What do the learned concepts look like?

Visualize the concept axes

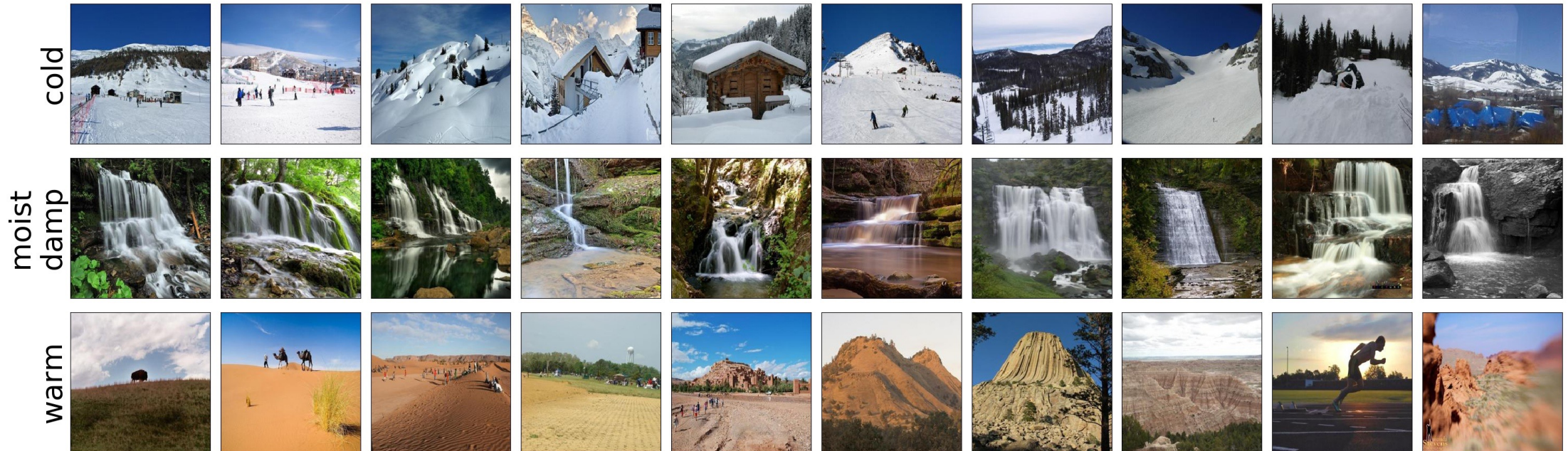
Most activated

16th layer



Visualize the concept axes

- Not only objects - weather

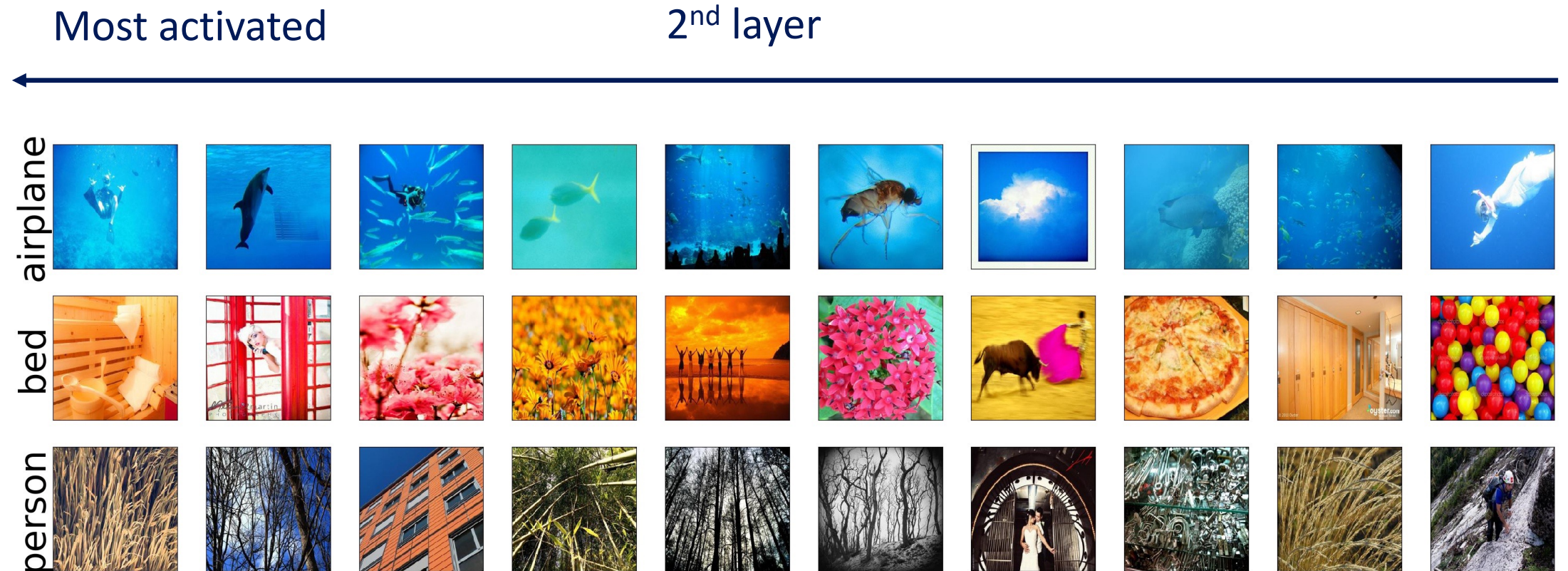


Visualize the concept axes

- Not only objects - material



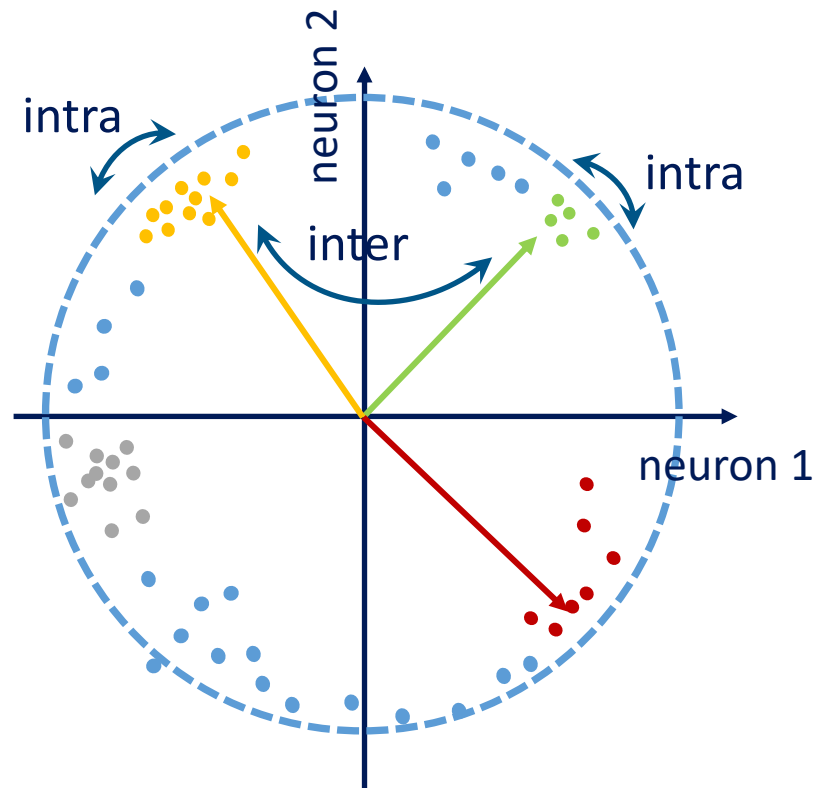
Visualize the concept axes



How to quantitatively measure the quality
of the learned concepts?

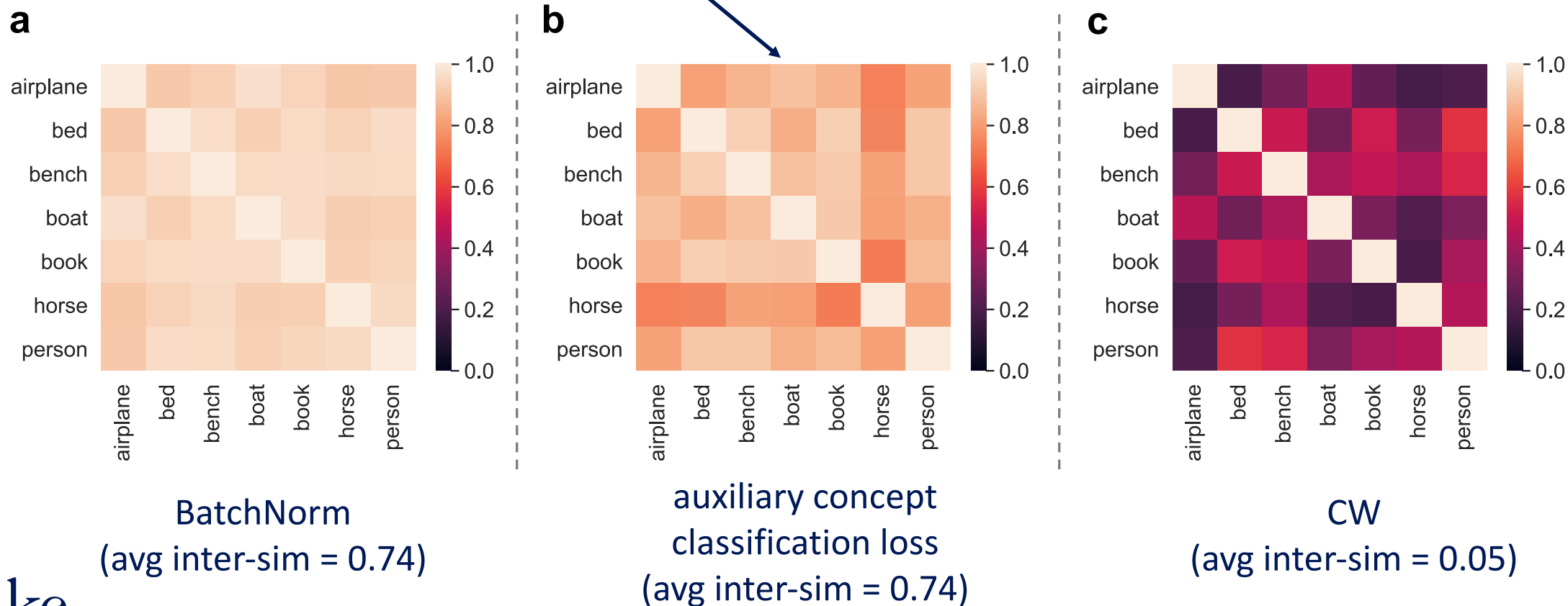
Concept separation

$$\text{inter- intra-concept ratio} = \frac{\text{avg cos similarity between concept } i \text{ and concept } j}{\sqrt{\text{avg cos similarity concept } i} \sqrt{\text{avg cos similarity concept } j}}$$



Concept separation

directly build a concept classifier in the latent space



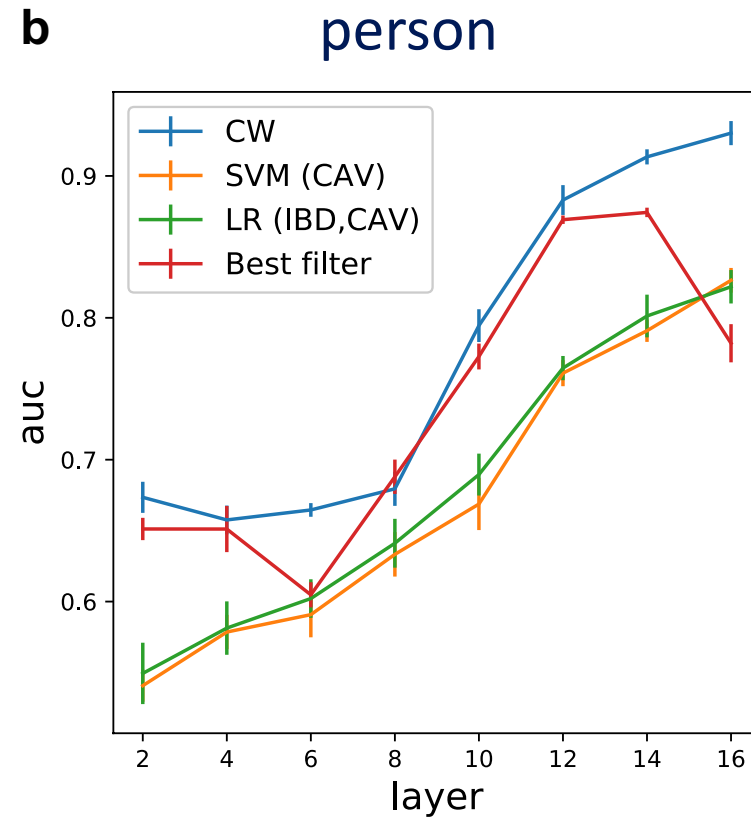
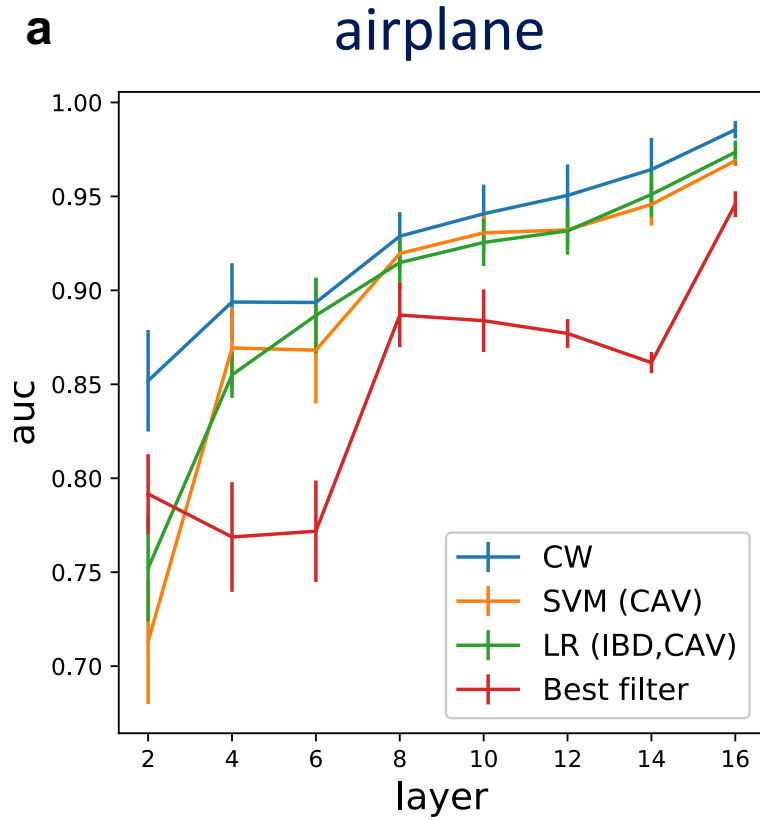
Concept purity

- airplane
- not airplane



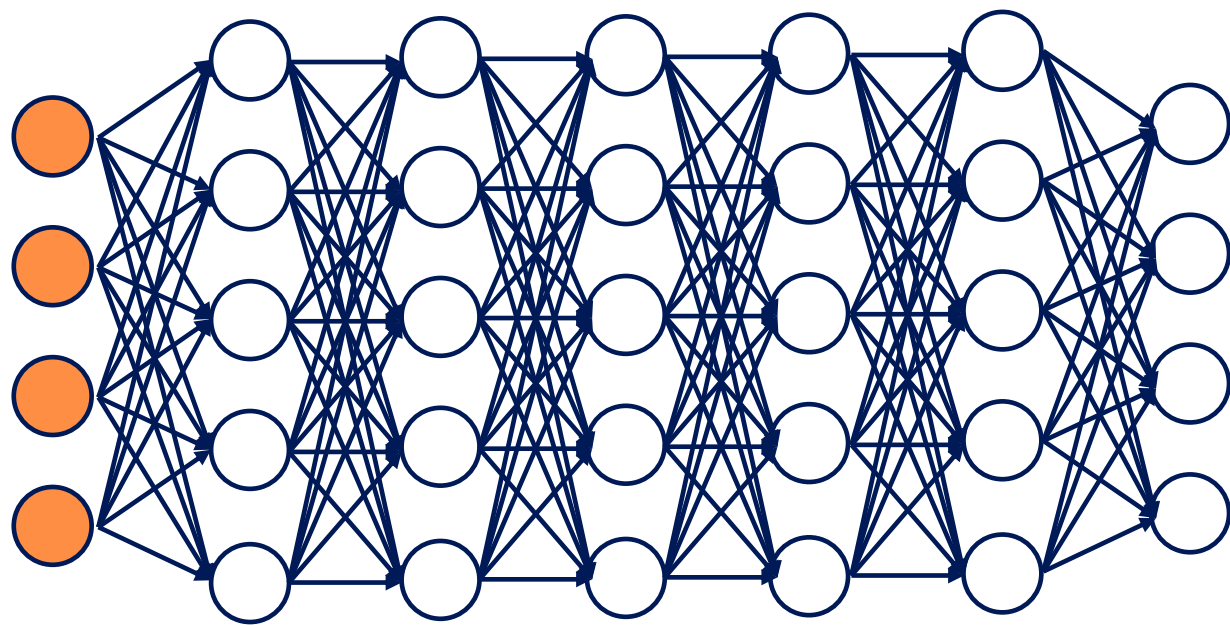
AUC of the activation measures concept purity

Concept purity

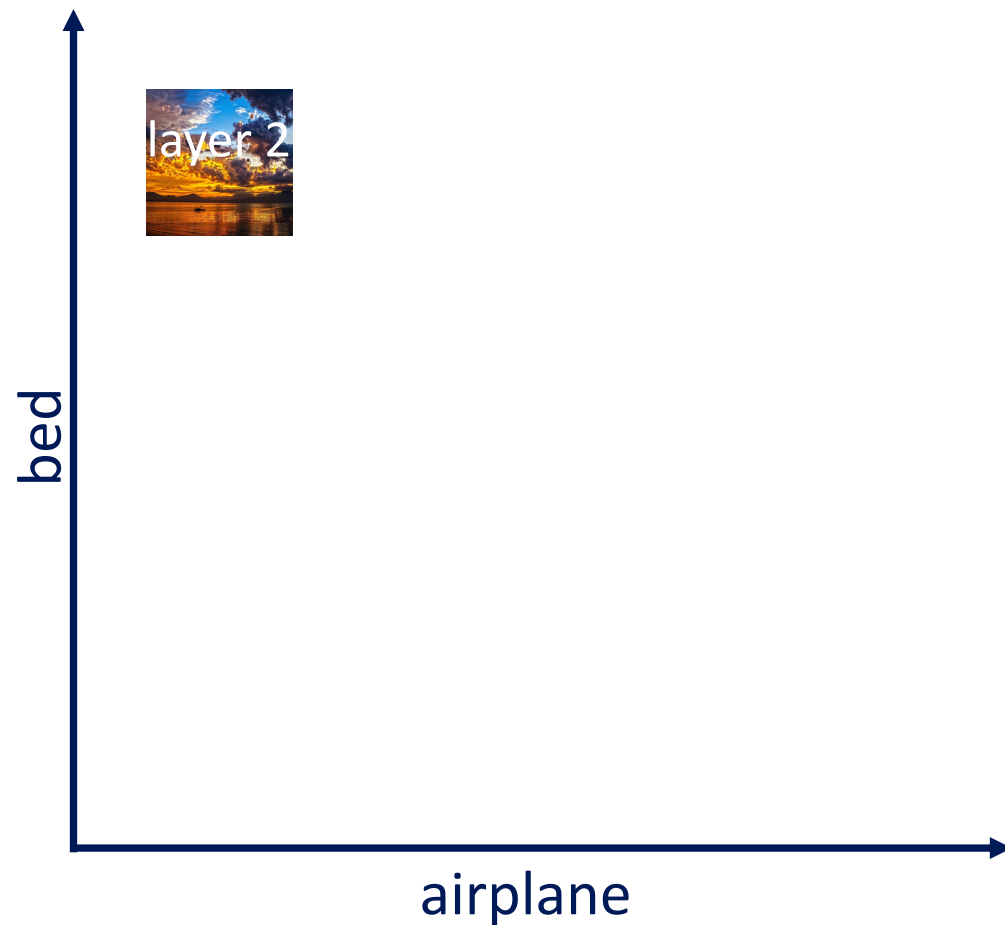


What can we use this model for?

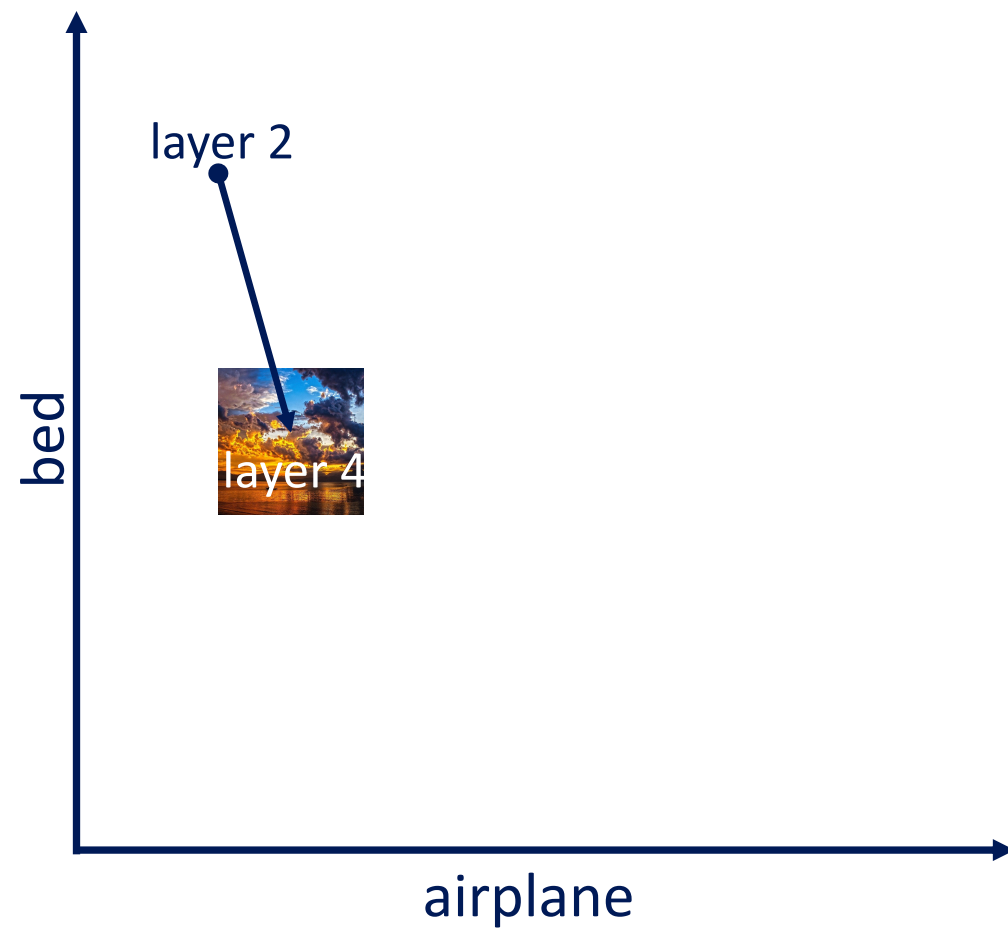
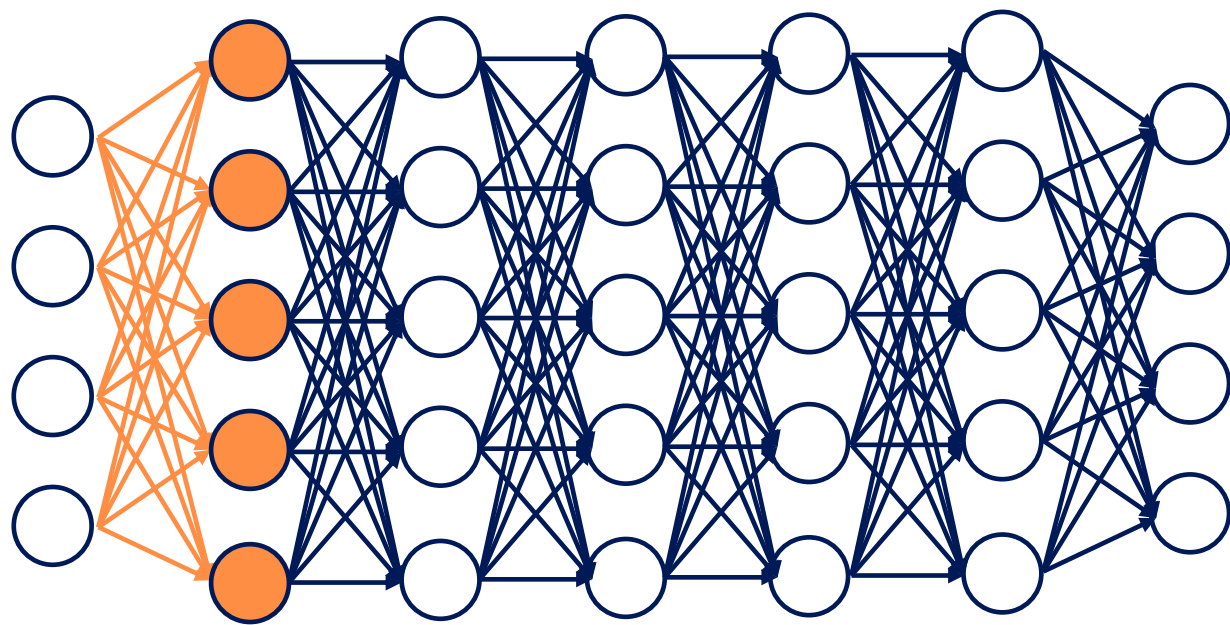
Reasoning process



Duke

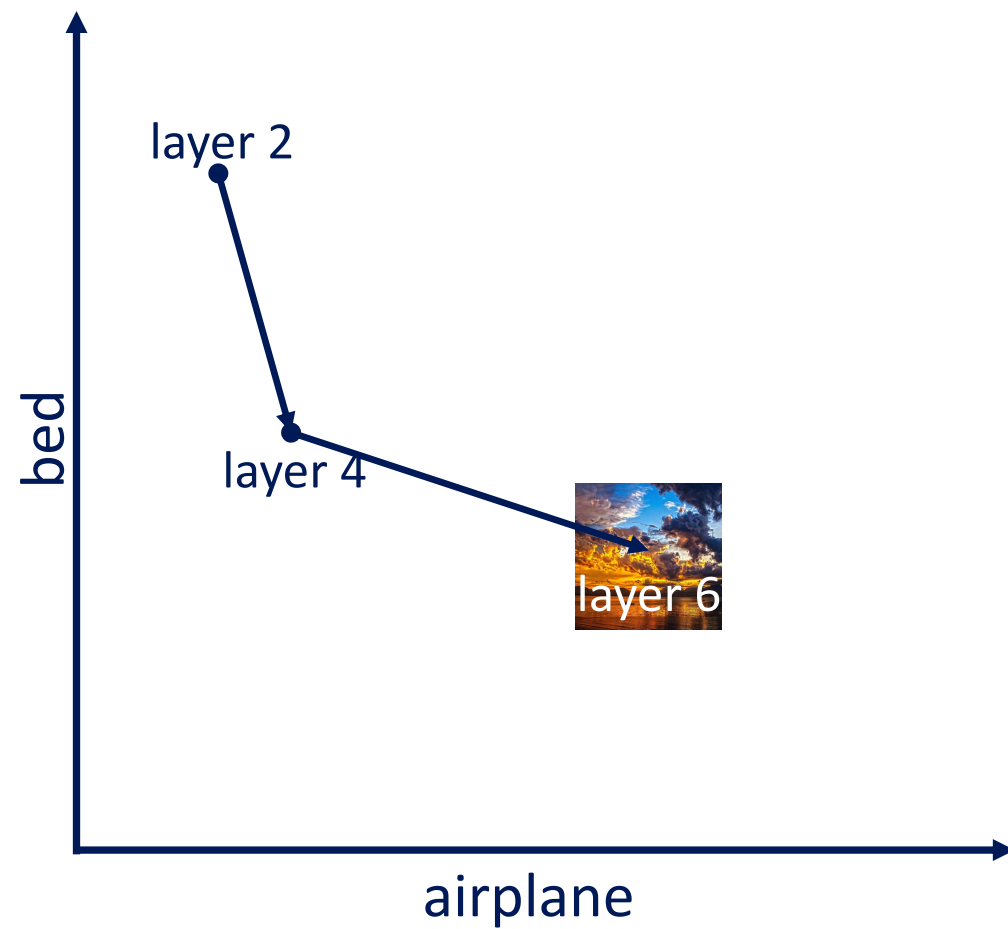
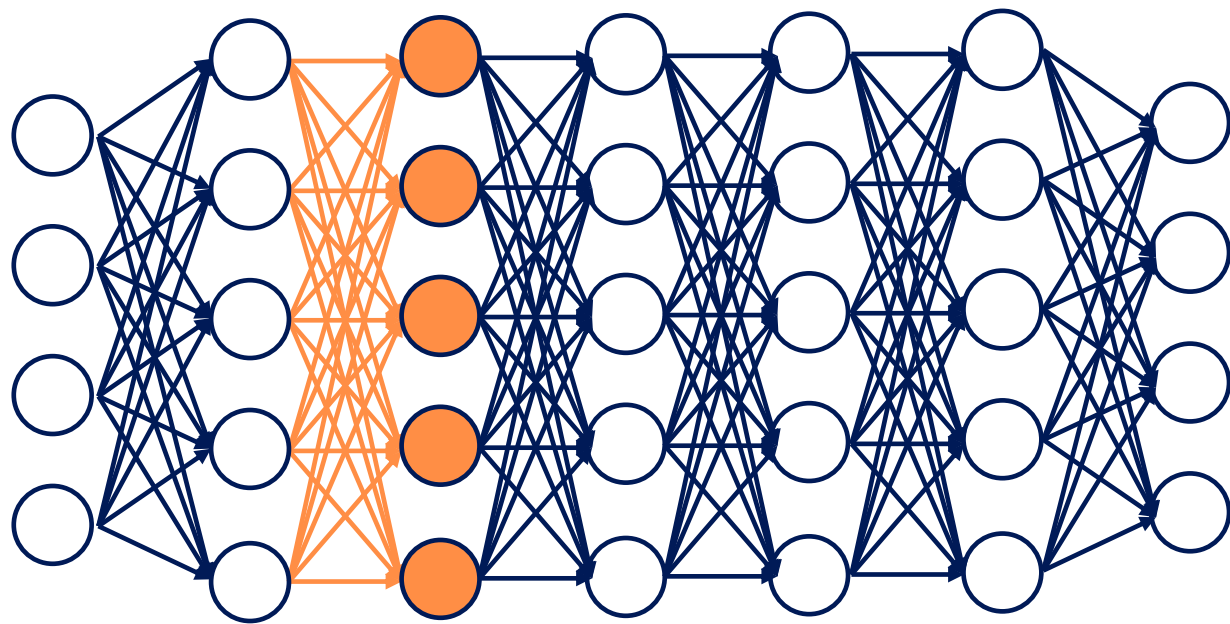


Reasoning process



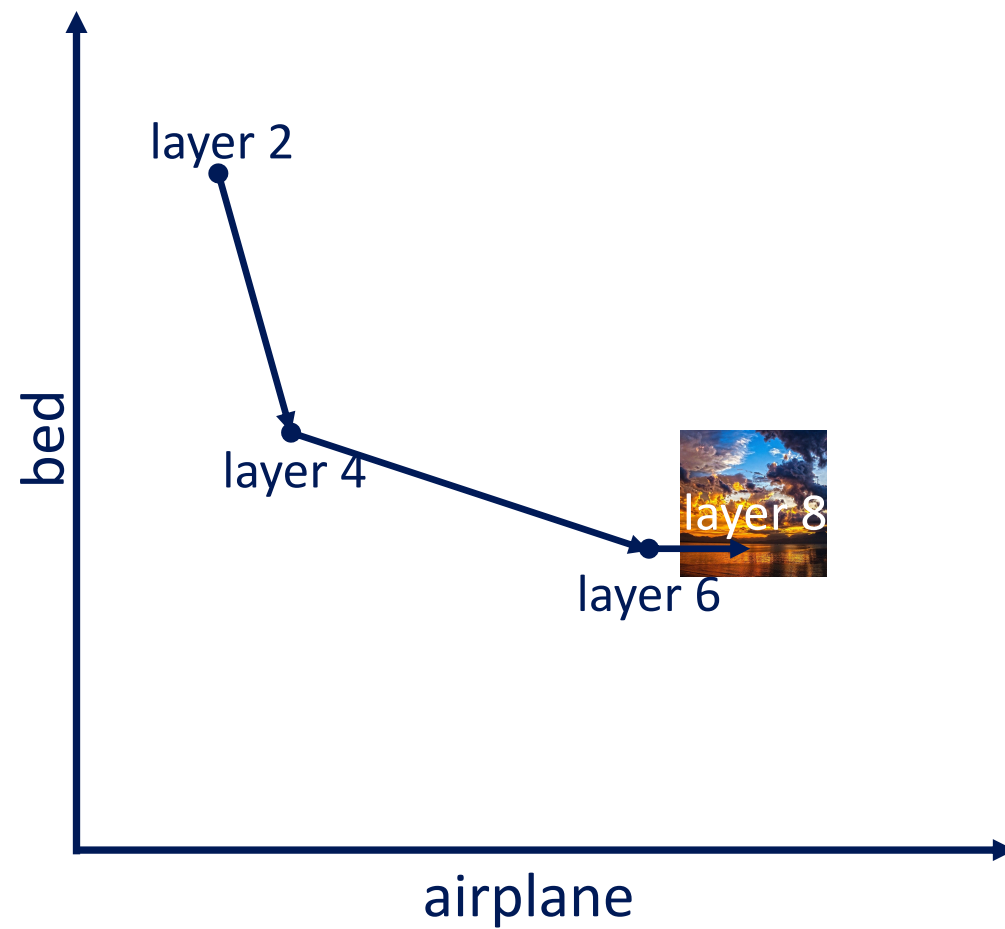
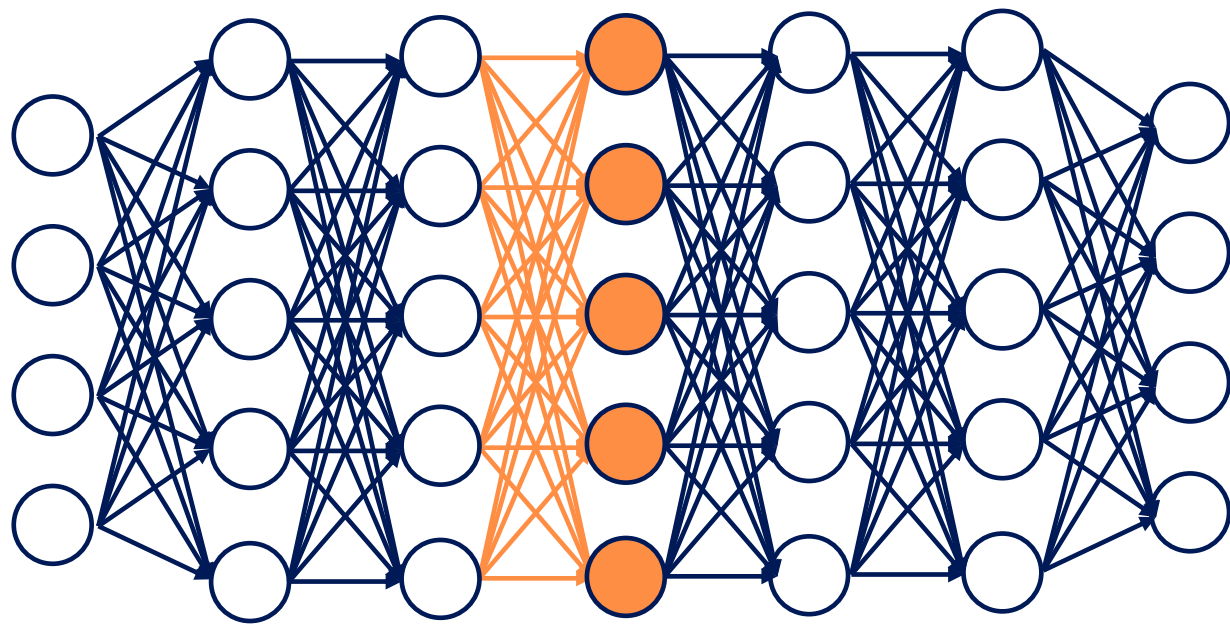
Duke

Reasoning process



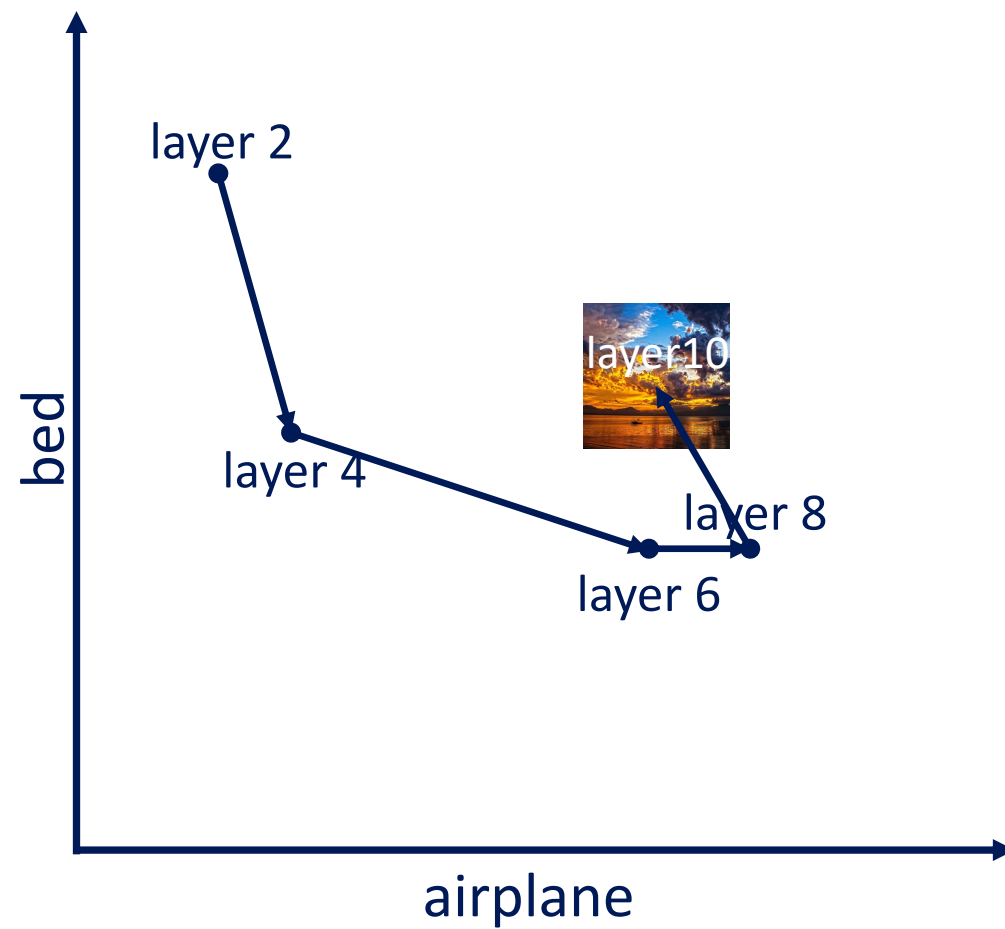
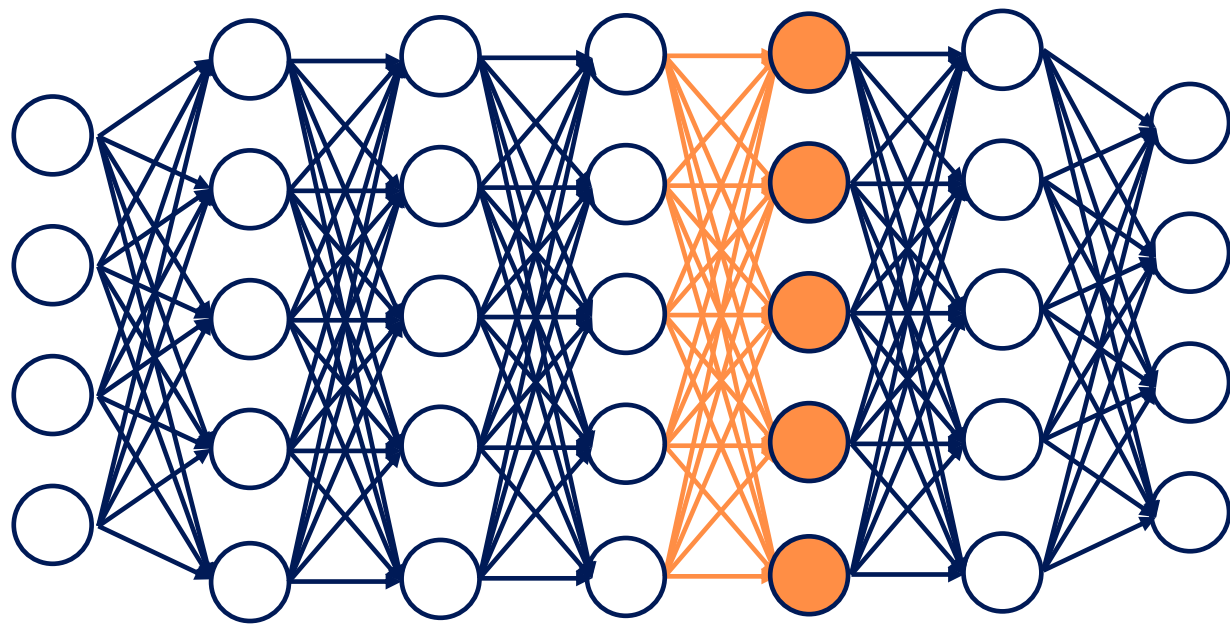
Duke

Reasoning process



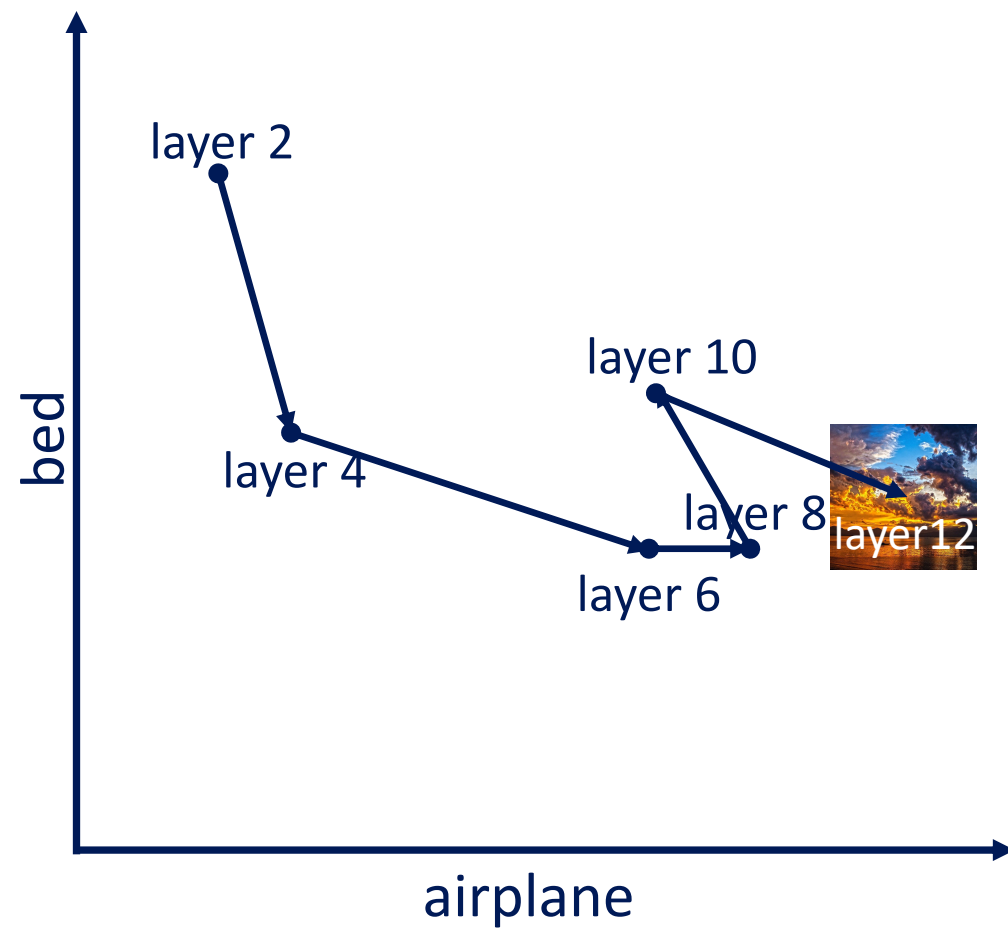
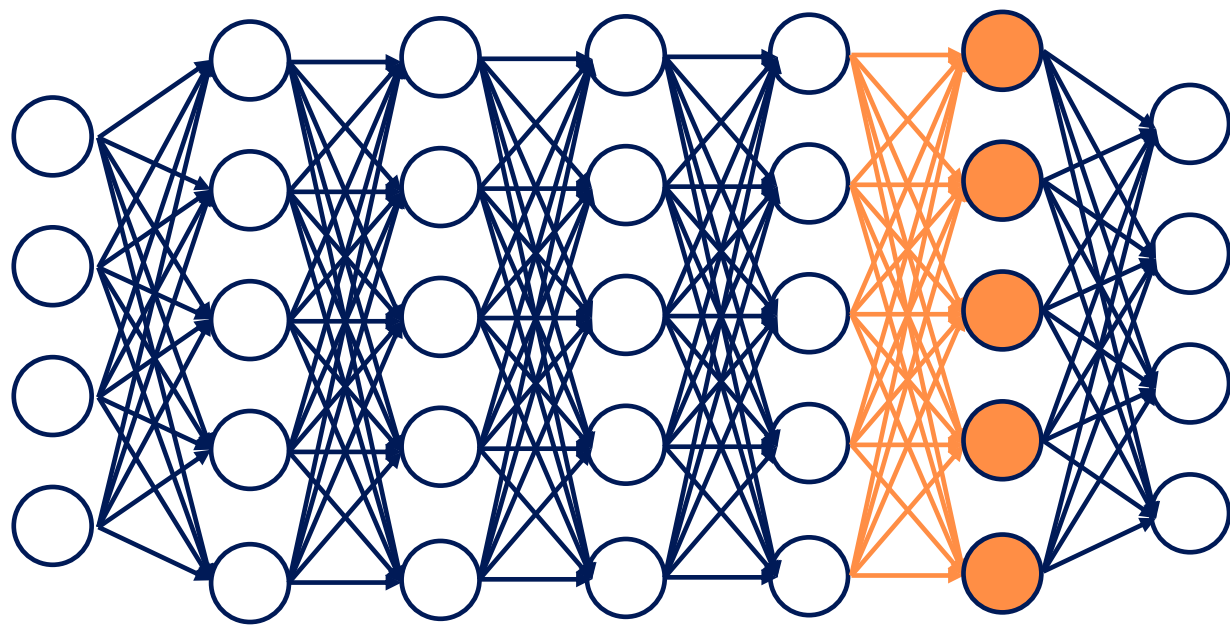
Duke

Reasoning process



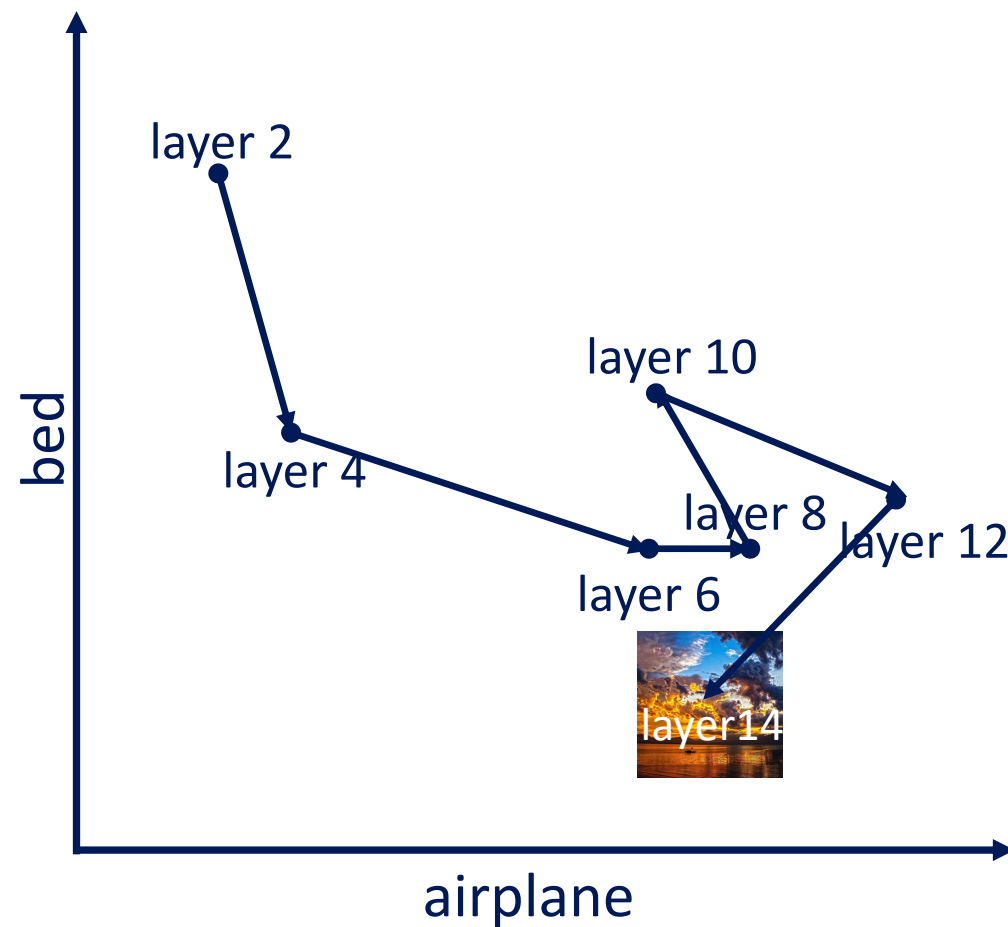
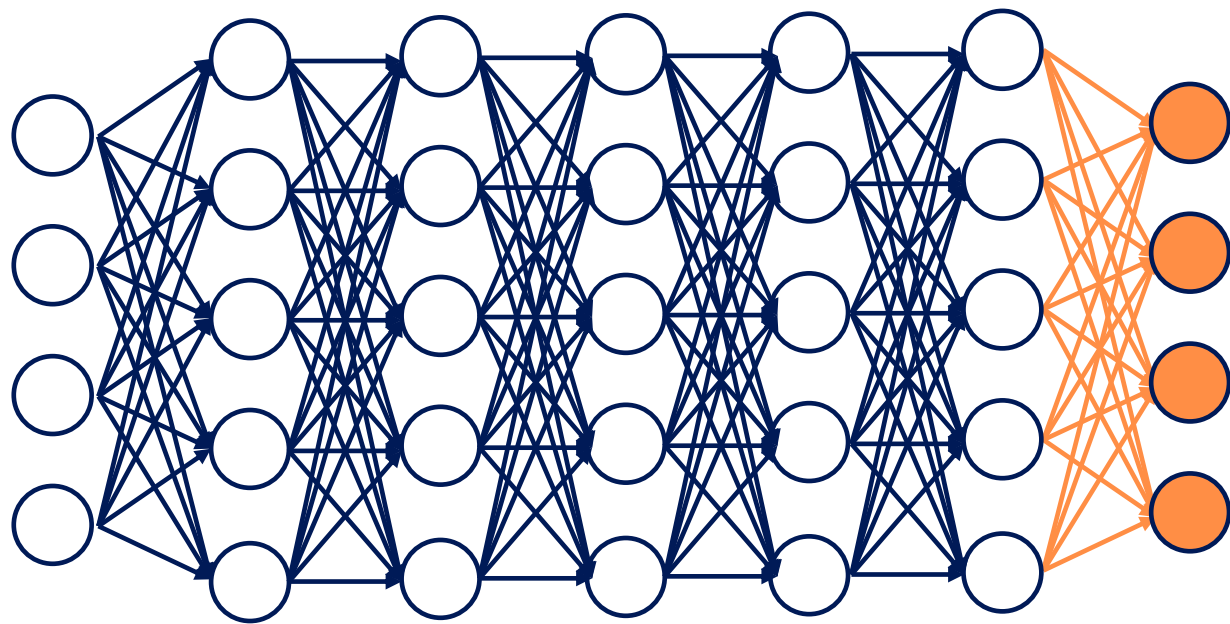
Duke

Reasoning process



Duke

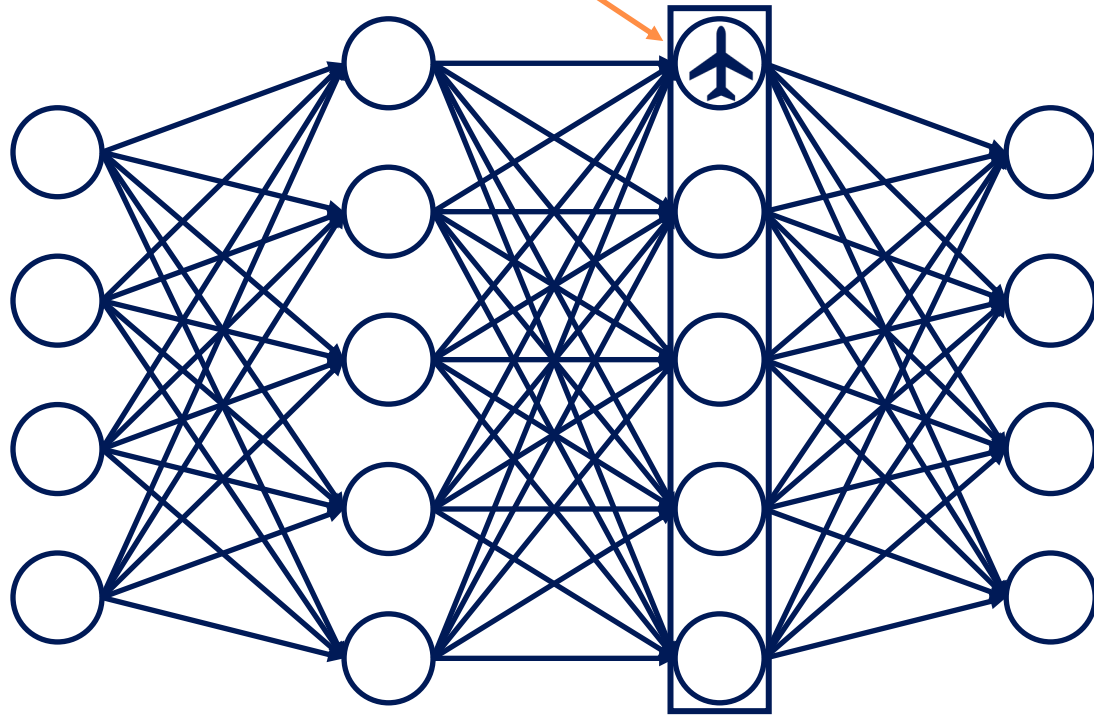
Reasoning process



Duke

Concept importance

permute the output

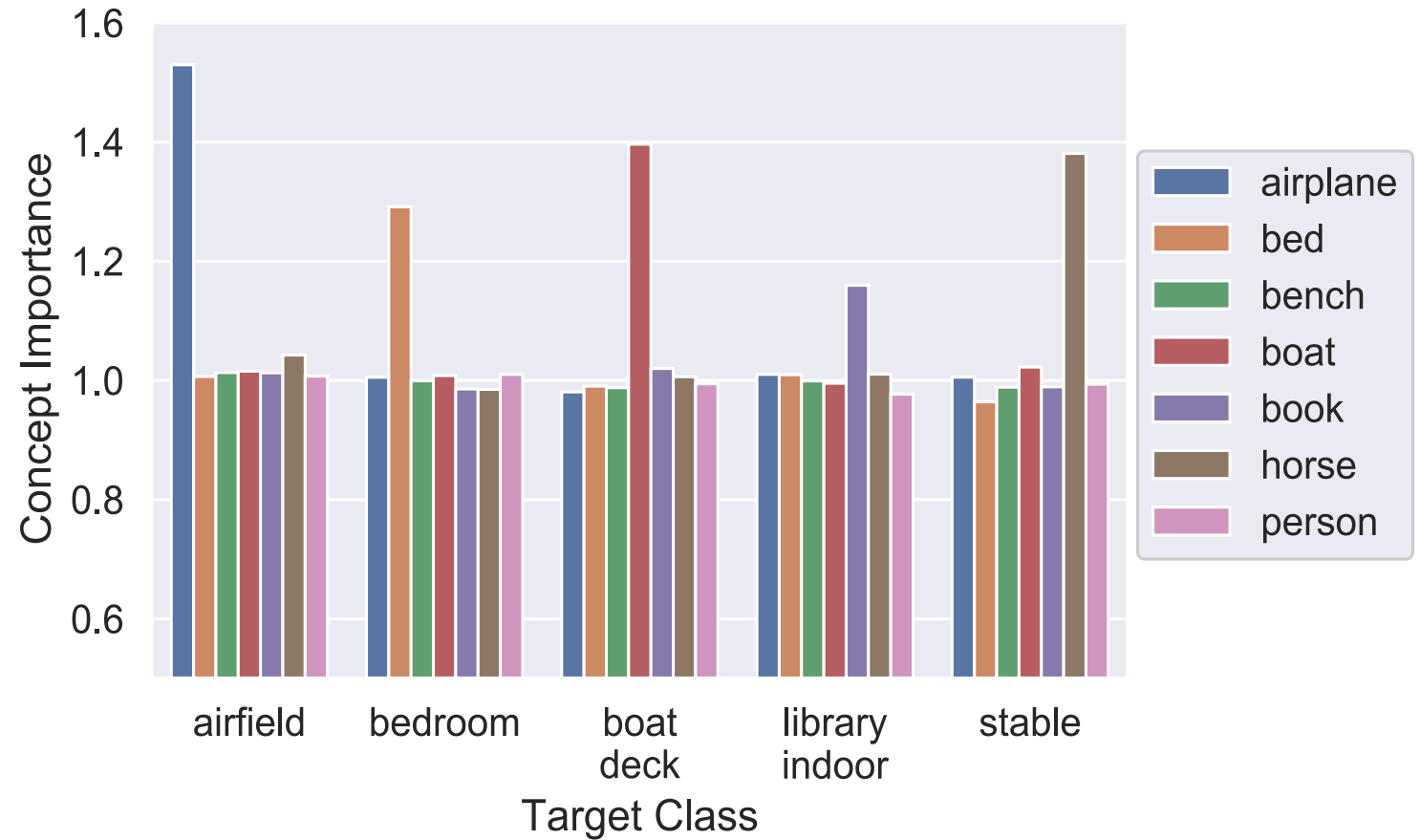


- Variable importance of axis j

$$CI_j = \frac{e_{\text{switch}}^{(j)}}{e_{\text{original}}}$$

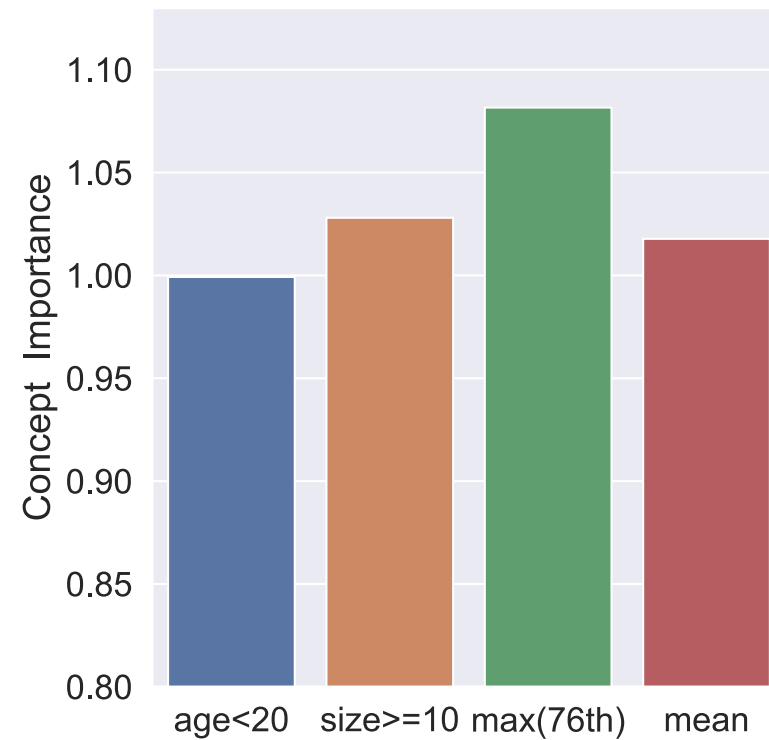
Concept importance

- Scene classification
 - Places365

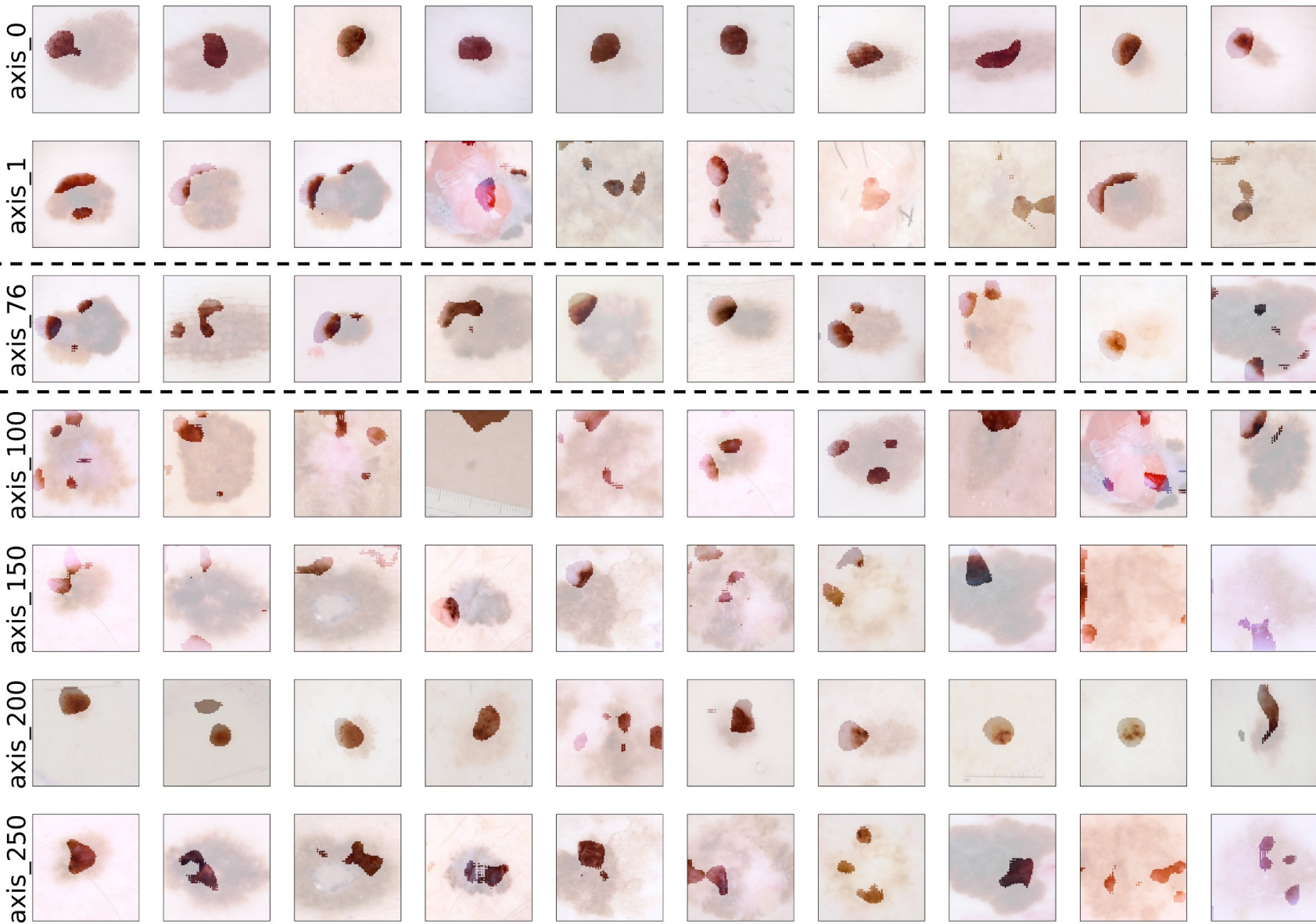


Concept importance

- Skin lesion malignancy
 - ISIC dataset
 - axis 1: age < 20
 - axis 2: size \geq 10 mm
 - not most important



Most Activated



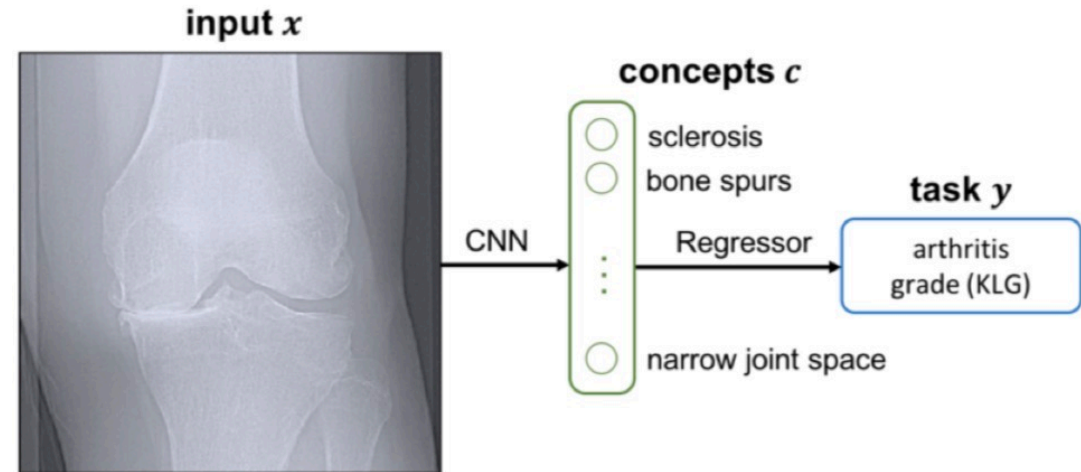
focused on boundaries



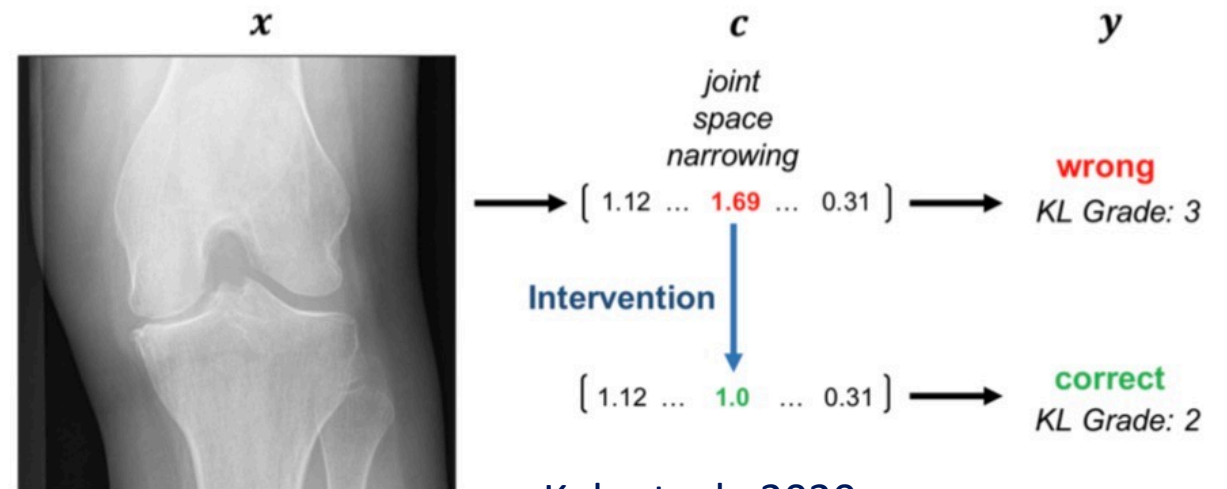
doctors also agree
boundary > size > age

Model intervention and editing

- Concept Bottleneck Model (Koh et. al , 2020)
 - they didn't disentangle
 - concept-based models can do test-time intervention



doctors can change the model when it is wrong



Koh et. al , 2020

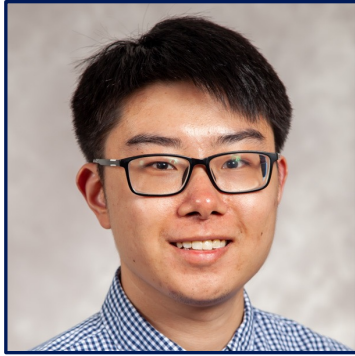
Summary: Concept Whitening

- Better interpretability
 - concepts are disentangled in the latent space
- No sacrifice in accuracy
 - accuracy is on par with standard CNNs
- Easy to use
 - warm-start from pretrained model requires only one additional epoch of further training

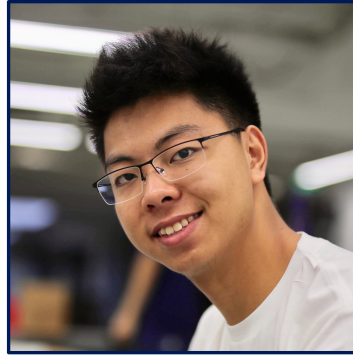
Links

- Nature Machine Intelligence paper
- <https://rdcu.be/cbOKj>
- Code
- <https://github.com/zhiCHEN96/ConceptWhitening>

Thank you



Zhi Chen



Yijie Bei



Cynthia Rudin

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