



# Correctness and Completeness for Incremental Model Synchronisation Based on TGGs

**BANFF Bidirectional Transformations**  
04-DECEMBER-2013



**Banff International Research Station**  
for Mathematical Innovation and Discovery

Frank Hermann, [frank.hermann@uni.lu](mailto:frank.hermann@uni.lu)

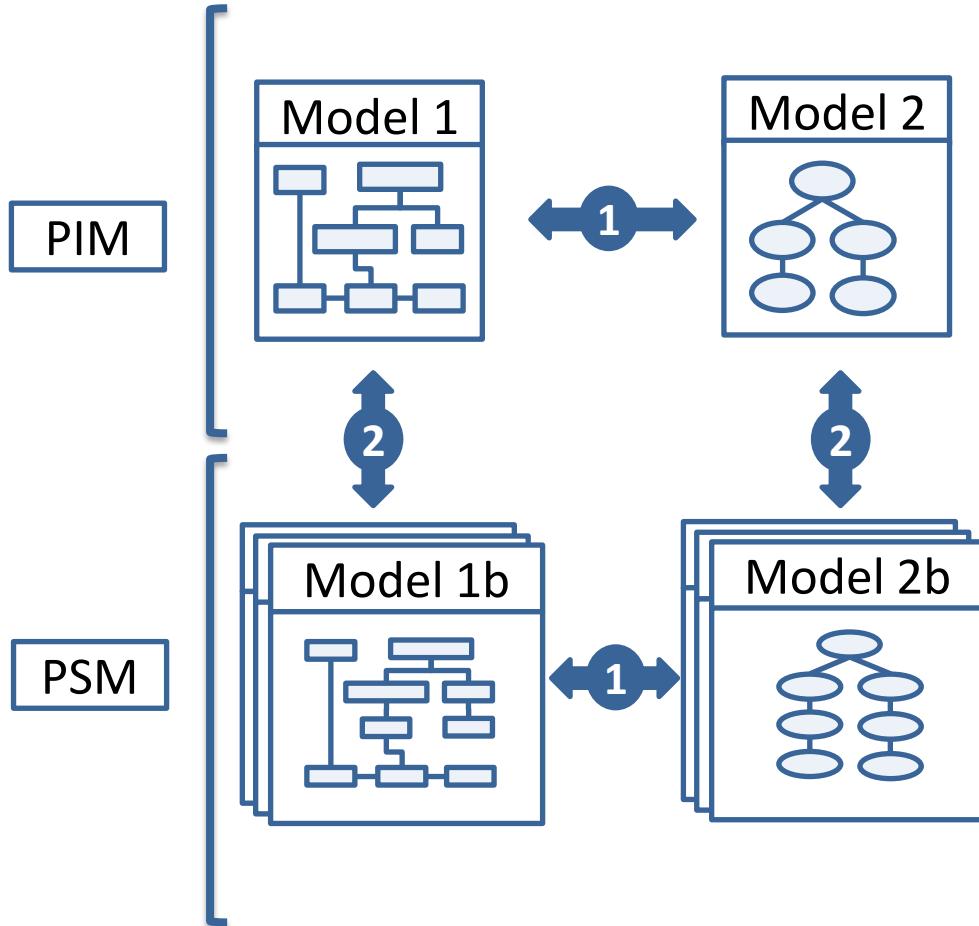
SECAN-Lab  
Interdisciplinary Centre for Security, Reliability and Trust  
Université du Luxembourg



# OVERVIEW

- **Formal results for model synchronization via TGGs**
- **Challenges for theory and tool support**
- Conclusion

# Interrelated Models in Model Driven Engineering



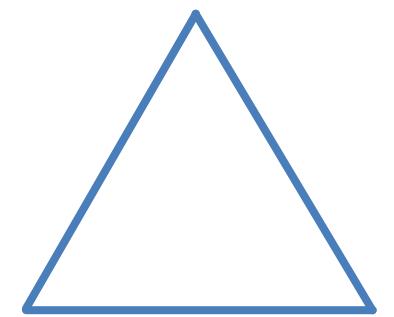
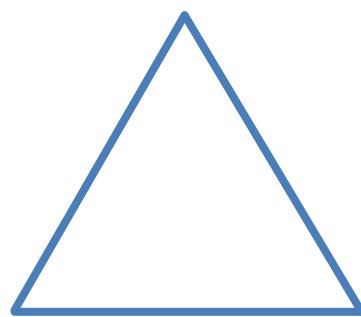
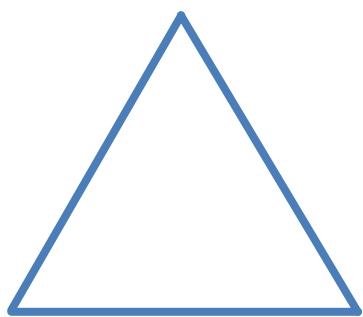
## Model Transformations

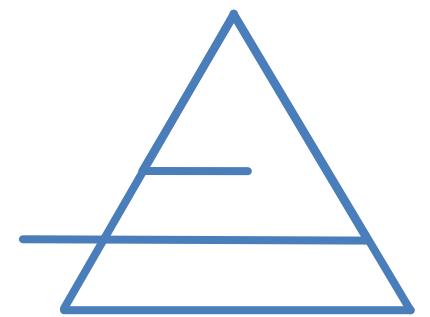
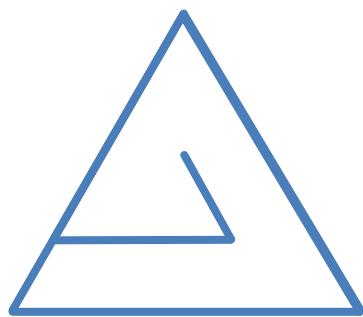
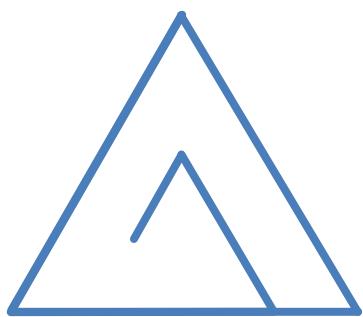
- 1 PIM↔PIM (horizontal):**  
DSL1↔DSL2,  
Model Translation/ Integration/  
Synchronisation, e.g.:  
**UML Class Diag.↔ RDBM**  
**BPMN ↔ BPEL**  
**Sequence Diag. ↔ St. Machines**
  
- 2 PIM↔PSM (vertical):**  
Model/Code generation,  
reverse engineering, e.g.:  
**Class Diag.↔Class Diag.**  
**Class Diag.↔Java**

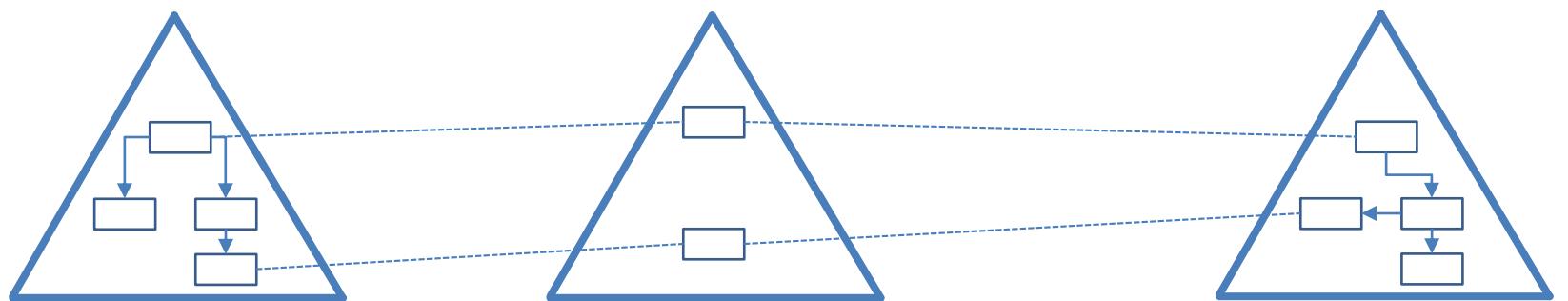
[HEO+13]





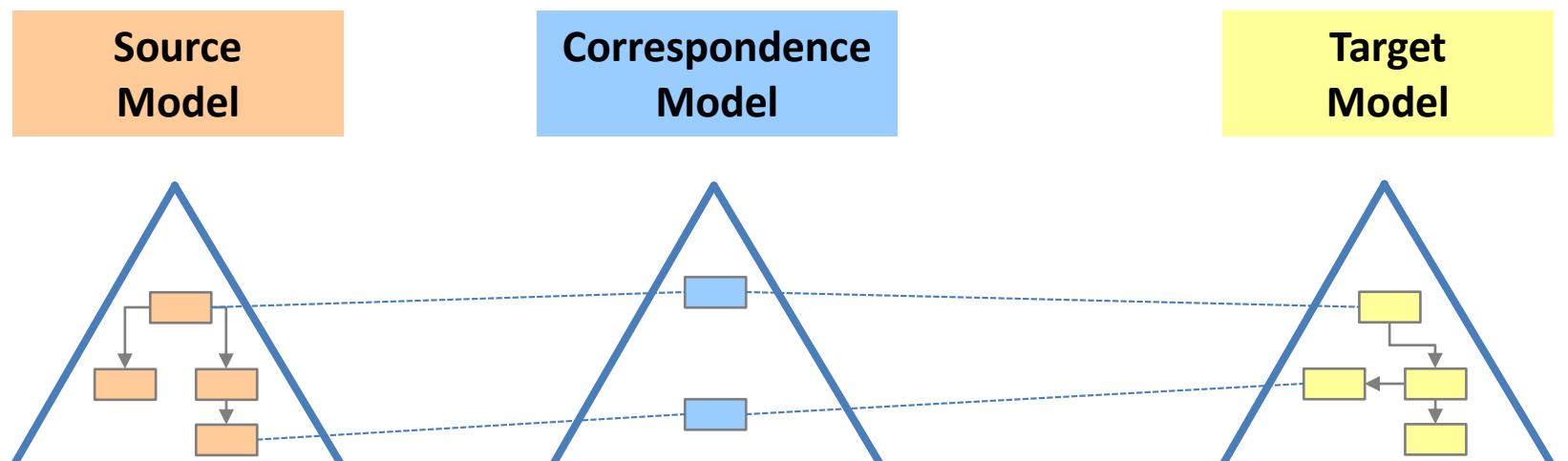






# Key Idea of Triple Graph Grammars (TGGs)

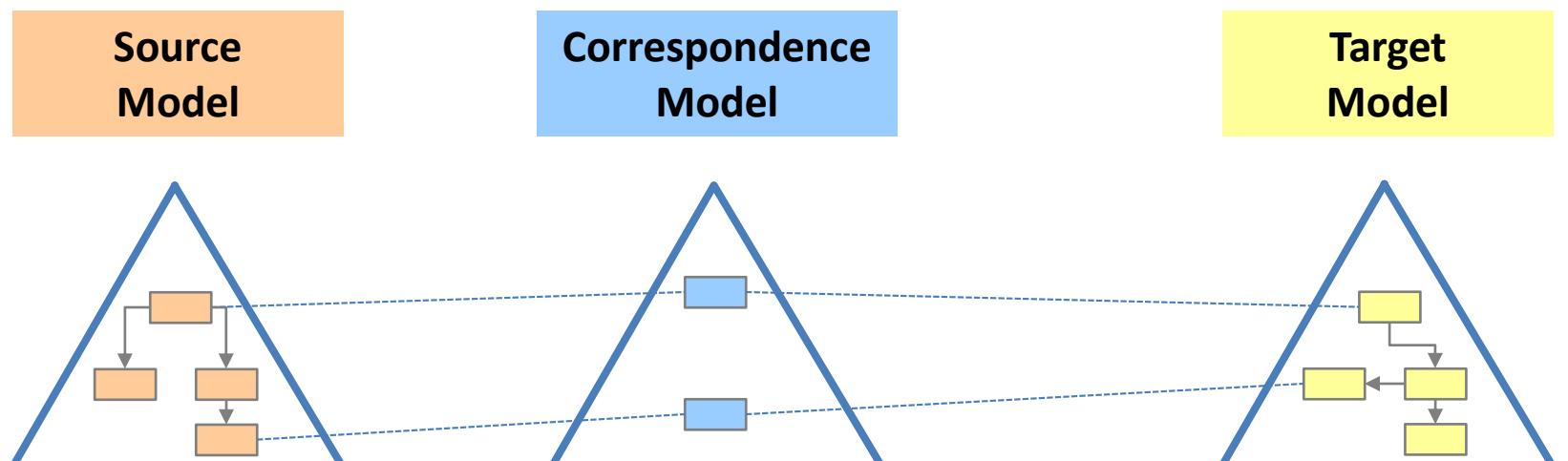
- **Specify** pattern by pattern how **consistent integrated models** can be constructed **simultaneously**



## Triple Graph

# Key Idea of Triple Graph Grammars (TGGs)

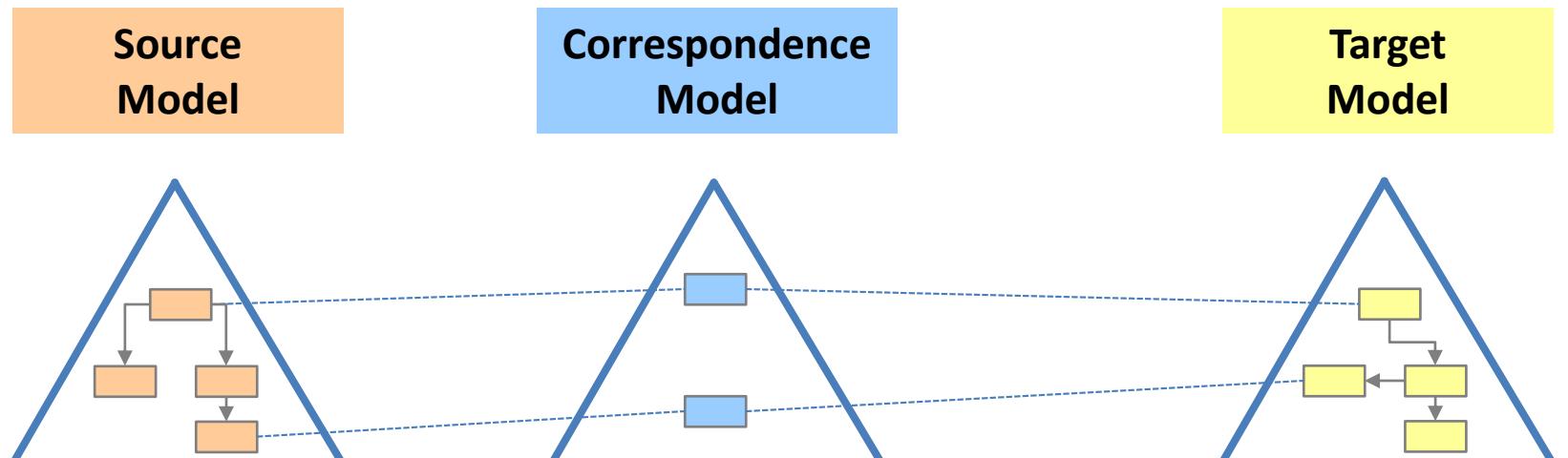
- **Specify** pattern by pattern how **consistent integrated models** can be constructed **simultaneously**
- **Generate** operations for interoperability:  
**Model Translation/Integration/Synchronisation**



**Triple Graph**

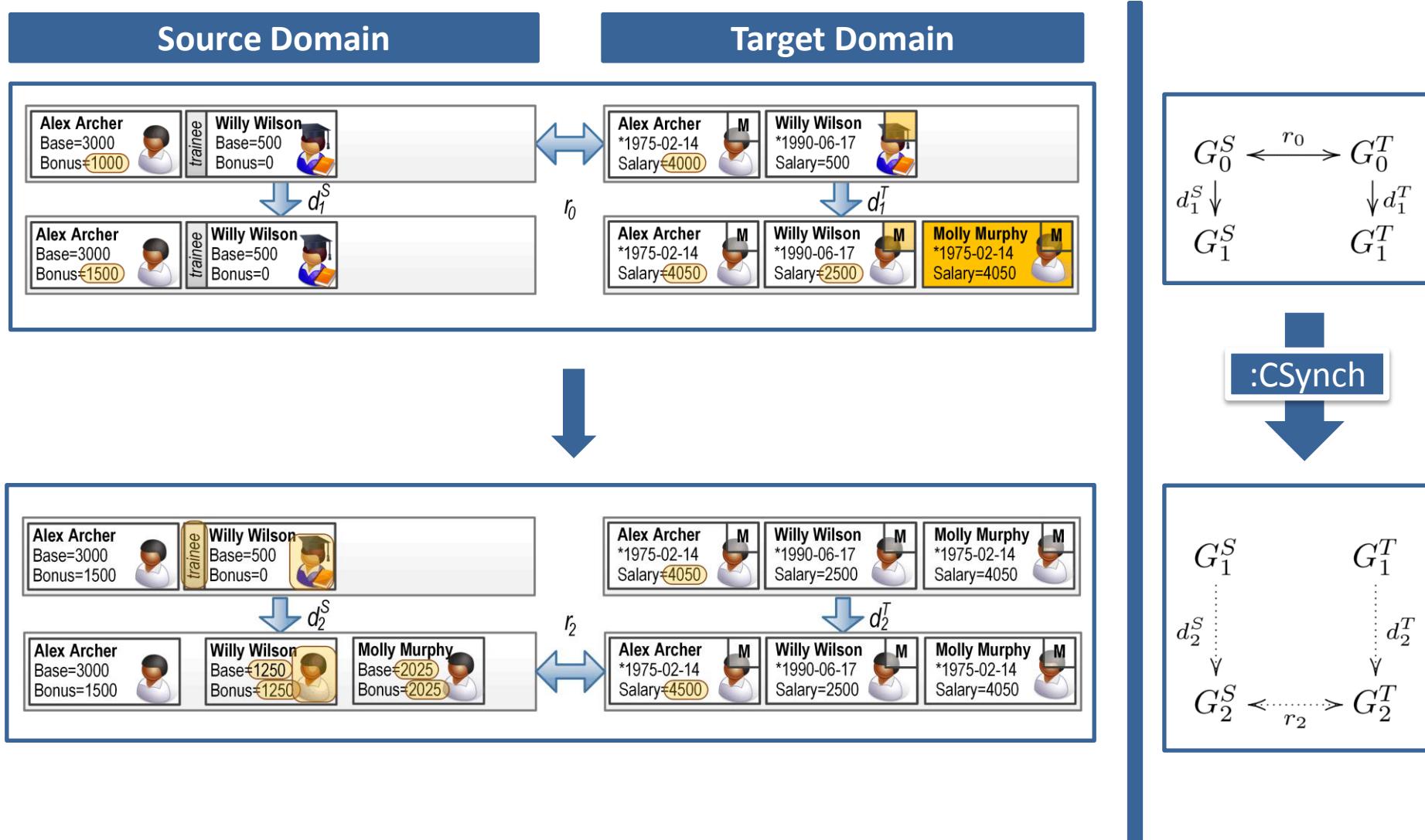
# Key Idea of Triple Graph Grammars (TGGs)

- **Specify** pattern by pattern how **consistent integrated models** can be constructed **simultaneously**
- **Generate** operations for interoperability:  
**Model Translation/Integration/Synchronisation**



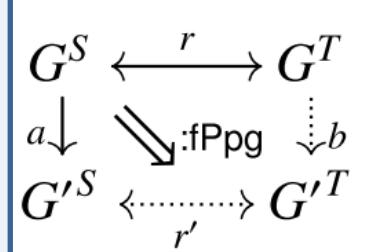
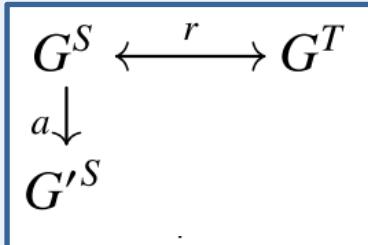
**Triple Graph**

# Concurrent Synchronization Problem

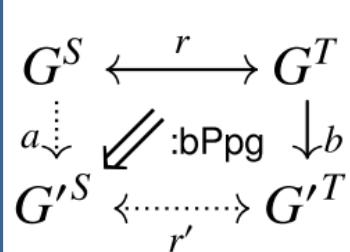
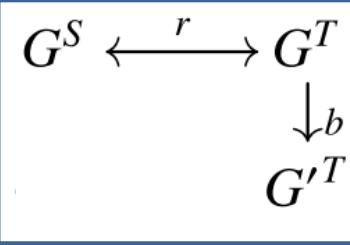


# Propagation

## Forward Propagation

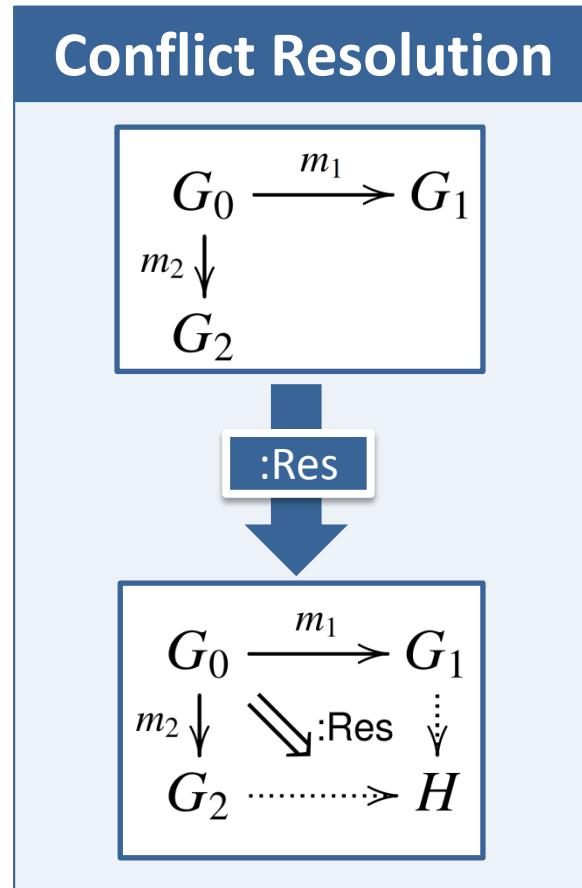


## Backward Propagation



- 
- [HEO+11] F. Hermann, H. Ehrig, F. Orejas, K. Czarnecki, Z. Diskin, Y. Xiong: Correctness of Model Synchronization Based on Triple Graph Grammars. In: Proc. MoDELS'11. Springer (2011).
- [HEO+13] F. Hermann, H. Ehrig, F. Orejas, K. Czarnecki, Z. Diskin, Y. Xiong, S. Gottmann, T. Engel: Model synchronization based on triple graph grammars: correctness, completeness and invertibility. In: Software & Systems Modeling, 1-29, Springer 2013.

# Conflict Resolution



## Resolution Strategy

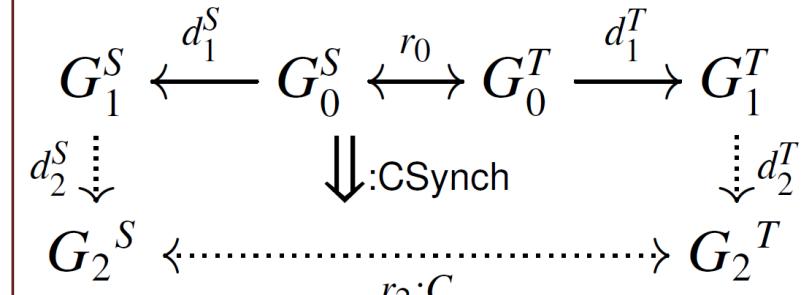
### Preservation over deletion

- Elements are **preserved**, if
  - **not deleted** by any update or
  - **required** by one update
- Elements are **deleted**, if:
  - **deleted** by one update and **not required** by the other
  - **deleted** by **both** updates

[EET11] H. Ehrig, C. Ermel, G. Taentzer: A Formal Resolution Strategy for Operation-Based Conflicts in Model Versioning Using Graph Modifications. In: Proc. FASE'11. Springer (2011).

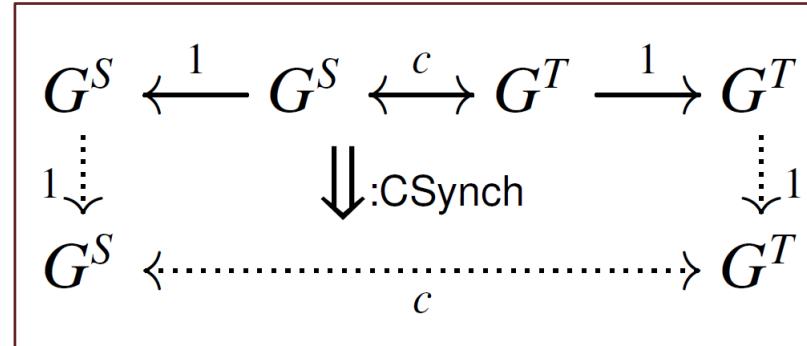
# Correctness

- ## 1. Consistency Law: result is always consistent



- ## 2. Identity Law:

no change, if input is already consistent



# Formal Result

## Definition (Completeness)

Model synchronisation can be performed for **any input**.

## Theorem (Correctness and Completeness)

The derived (non-) deterministic concurrent synchronisation framework CSync(TGG, CSync) is **correct** and **complete**.

---

[GHN+13] S Gottmann, F Hermann, N Nachtigall, B Braatz, C Ermel, H Ehrig, T Engel: Correctness and Completeness of Generalised Concurrent Model Synchronisation Based on Triple Graph Grammars. In: Proc. AMT'13, CEUR 2013.

[HEEO12] H. Ehrig, C. Ermel, G. Taentzer: Concurrent Model Synchronization with Conflict Resolution Based on Triple Graph Grammars. In: Proc. FASE'12. Springer (2012).

# Existing Implementations

## Achievement

**Incremental synchronization** – making it applicable in practice (non-invasive and efficient)

## Restriction

**Concurrency:** no concurrent updates that could cause conflicts

## Restriction

**Types of TGGs:** e.g., deterministic, node creating rules, rule dependencies

# Key Challenges

## Problem

**Diversity:** different concepts and implementations for incremental propagation

## Challenge

Provide a **generalized notion** of incremental propagation (least change)

## Problem

**Gap:** between formal results and implementations of incremental synchronisation

## Challenge

**Extend formal approaches** to achieve a close relation to implementations

## Challenge

**Extend implementations** to the concurrent case

# Conclusion and next steps

## SUMMARY

- Concurrent model synchronisation via TGGs
- Guarantees: syntactical correctness, completeness, termination

## NEXT STEPS

- Closing the gap between formal theory and implementations by extending both

# Further Reading

[EEE+07]	H. Ehrig, K. Ehrig, C. Ermel, F. Hermann, and G. Taentzer: <b>Information Preserving Bidirectional Model Transformations.</b> <i>Proc. FASE'07</i> . Springer (2007).
[EEPT06]	H. Ehrig, K. Ehrig, U. Prange, and G. Taentzer: <b>Fundamentals of Algebraic Graph Transformation.</b> EATCS Monographs in Theoretical Computer Science. Springer (2006).
[GHL12]	Giese, H., Hildebrandt, S., Lambers, L.: <b>Bridging the Gap Between Formal Semantics and Implementation of Triple Graph Grammars. Ensuring Conformance of Relational Model Transformation Specifications and Implementations.</b> <i>Software and Systems Modeling</i> , Springer (2012).
[GW09]	Giese, H., Wagner, R.: <b>From model transformation to incremental bidirectional model synchronization.</b> <i>Software and Systems Modeling</i> 8(1), Springer (2009).
[HEGO10]	F. Hermann, H. Ehrig, U. Golas, Fernando Orejas: <b>Efficient Analysis and Execution of Correct and Complete Model Transformations Based on Triple Graph Grammars.</b> <i>Proc. of MDI'10</i> , ACM (2010).
[HEOG10]	F. Hermann, H. Ehrig, F. Orejas, U. Golas: <b>Formal analysis of functional behaviour for model transformations based on triple graph grammars.</b> In: <i>Int. Conf. on Graph Transformations</i> , Springer (2010).

# Further Reading

[HEO+13]	F. Hermann, H. Ehrig, F. Orejas, K. Czarnecki, Z. Diskin, Y. Xiong, S. Gottmann, T. Engel: <b>Model synchronization based on triple graph grammars: correctness, completeness and invertibility.</b> In: Software & Systems Modeling, Springer 2013.
[KW07]	Kindler, E., Wagner, R.: <b>Triple graph grammars. concepts, extensions, implementations, and application scenarios.</b> Tech. Rep. TR-ri-07-284, Department of Computer Science, University of Paderborn (2007).
[LAVS12]	Lauder, M., Anjorin, A., Varró, G., Schürr, A.: Bidirectional model transformation with precedence triple graph grammars. In: <i>Proc. Eur. Conf. on Modelling Foundations and Applications (ECMFA'12)</i> , LNCS, vol. 7349. Springer (2012).
[Schürr94]	Schürr, A.: <b>Specication of Graph Translators with Triple Graph Grammars.</b> Proc. of WG 1994. LNCS, Springer (1995).
[SK08]	Schürr, A., Klar, F.: 15 years of triple graph grammars. In: <i>Int. Conf. on Graph Transformations (ICGT 2008)</i> . LNCS, vol. 5214, Springer (2008).