

(Erdős-de Bruijn) $\text{Chr}(X) \leq n$ iff
every finite subgraph has chromatic
number $\leq n$ ($n < \omega$)

Every graph has a chromatic
number iff AC